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**Real-Time Volume Graphics**

# [13] Non-Photorealistic and Illustrative Techniques

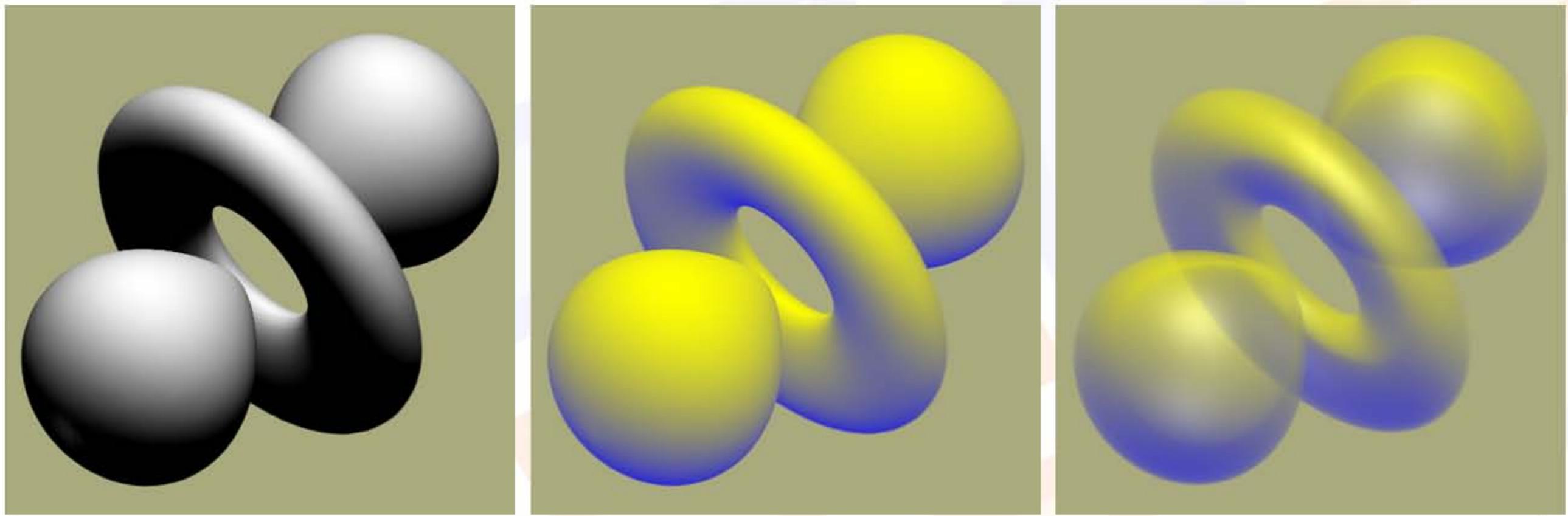


# Tone Shading (1)

Mimic style of artistic illustrations [Gooch et al. '98]

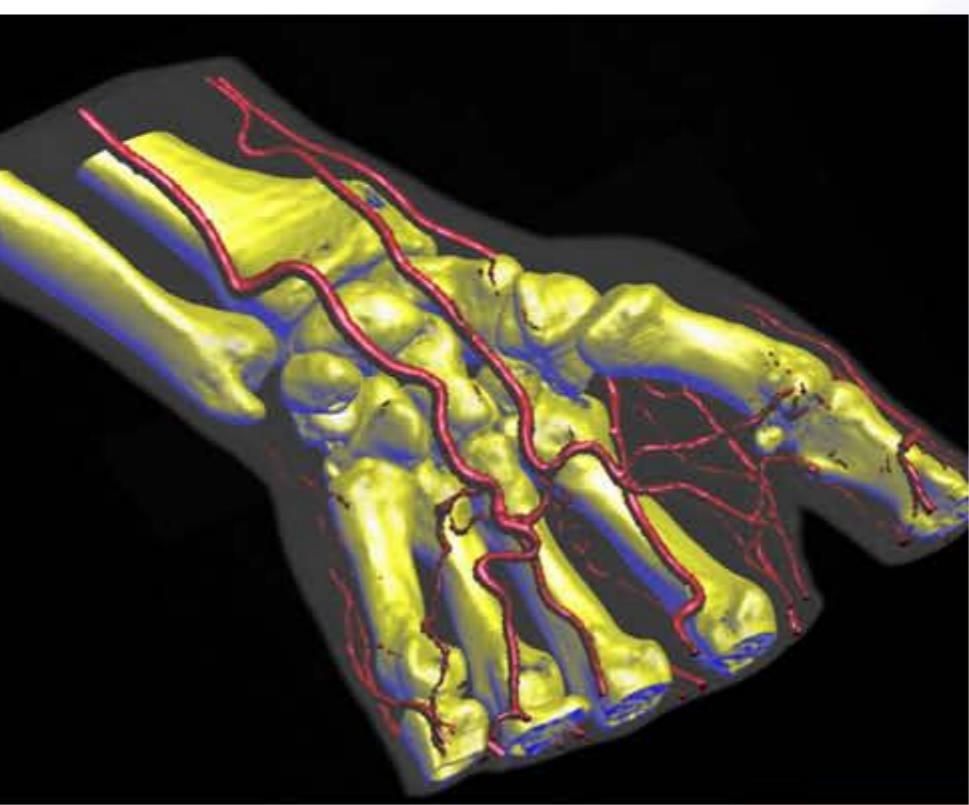
- Interpolate between two colors: better depth perception

$$\mathbf{I} = \left( \frac{1 + \mathbf{l} \cdot \mathbf{n}}{2} \right) k_a + \left( 1 - \frac{1 + \mathbf{l} \cdot \mathbf{n}}{2} \right) k_b$$



# Tone Shading (2)

- Colors from transfer function plus cool/warm tones
- Opacity directly from transfer function



$$k_a = k_{cool} + \alpha k_t$$

$$k_b = k_{warm} + \beta k_t$$

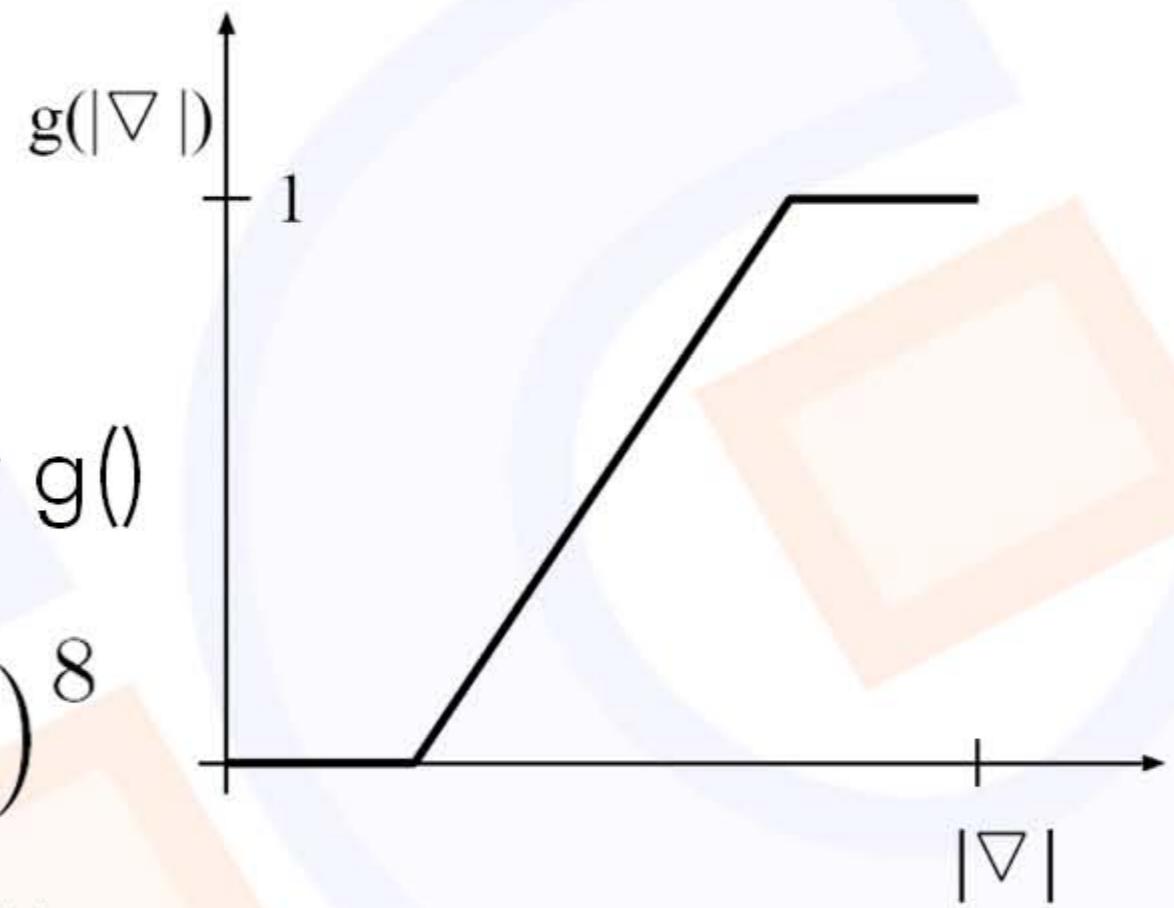


# Volumetric Boundary Contours (1)

Based on view direction and gradient magnitude  
[Csebfalvi et al., EG 2001], [Ebert et al., Vis 2001]

- Global boundary detection instead of isosurface
- Gradient magnitude window  $g()$

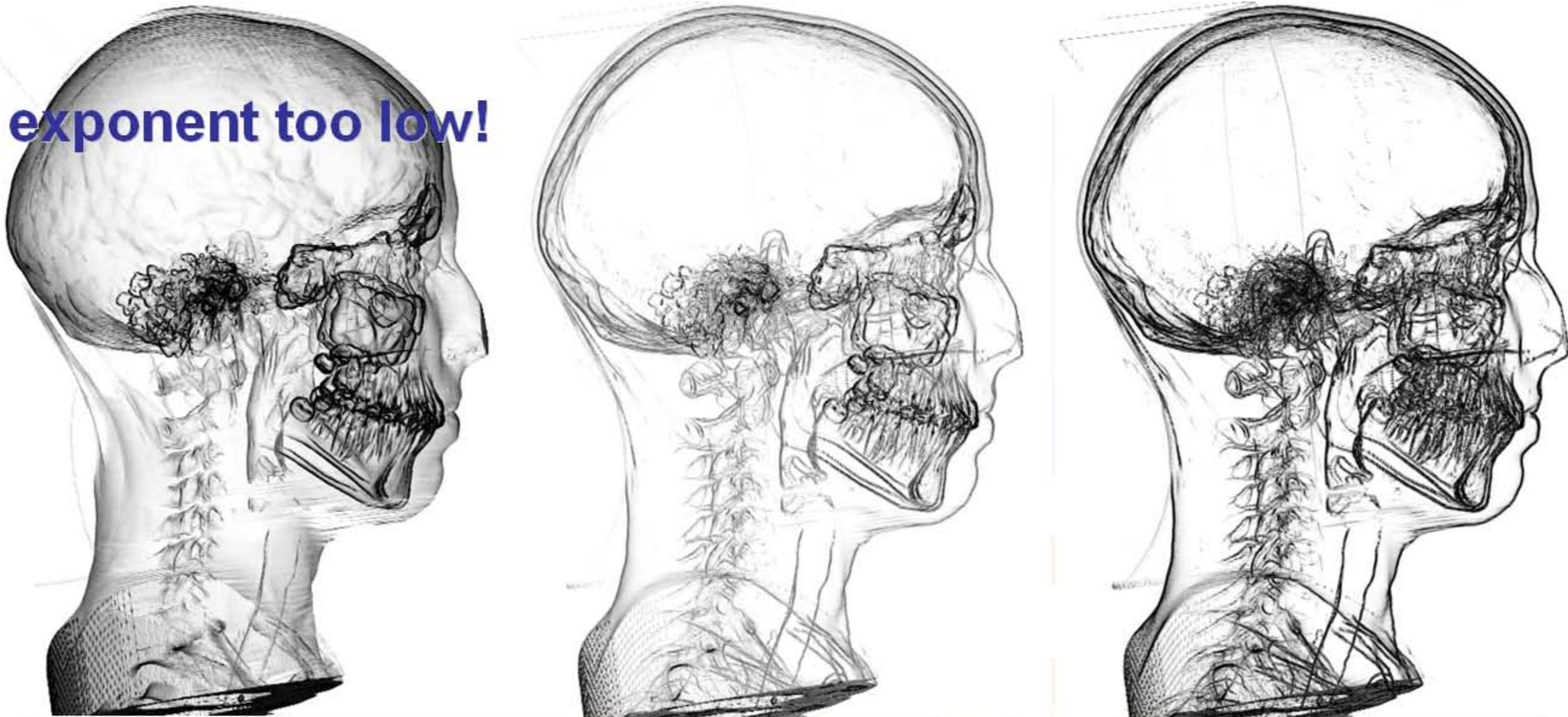
$$I = g(|\nabla f|) \cdot (1 - |\mathbf{v} \cdot \mathbf{n}|)^8$$



- Exponent determines silhouette range
- Does not work for distance fields!

# Volumetric Boundary Contours (2)

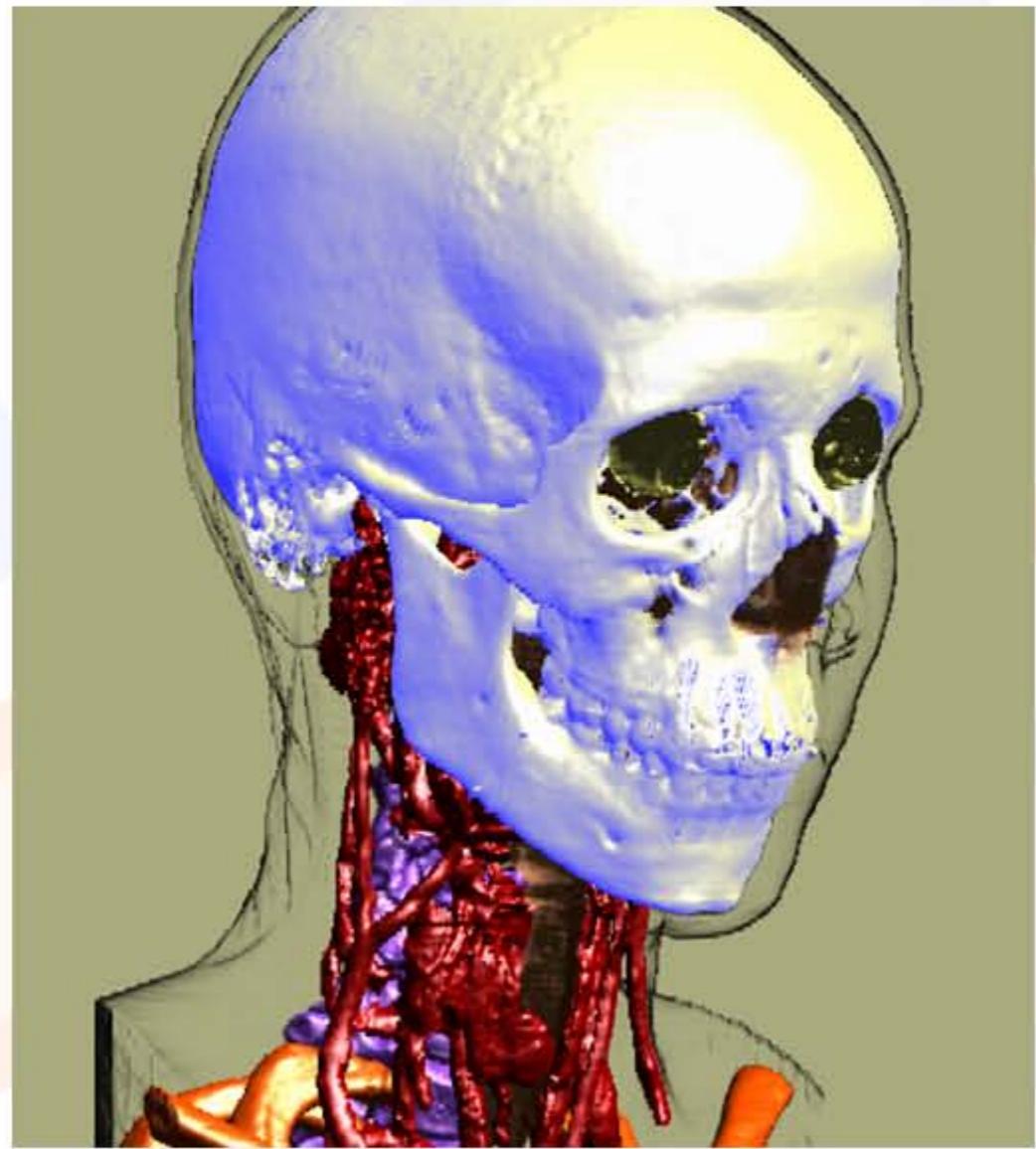
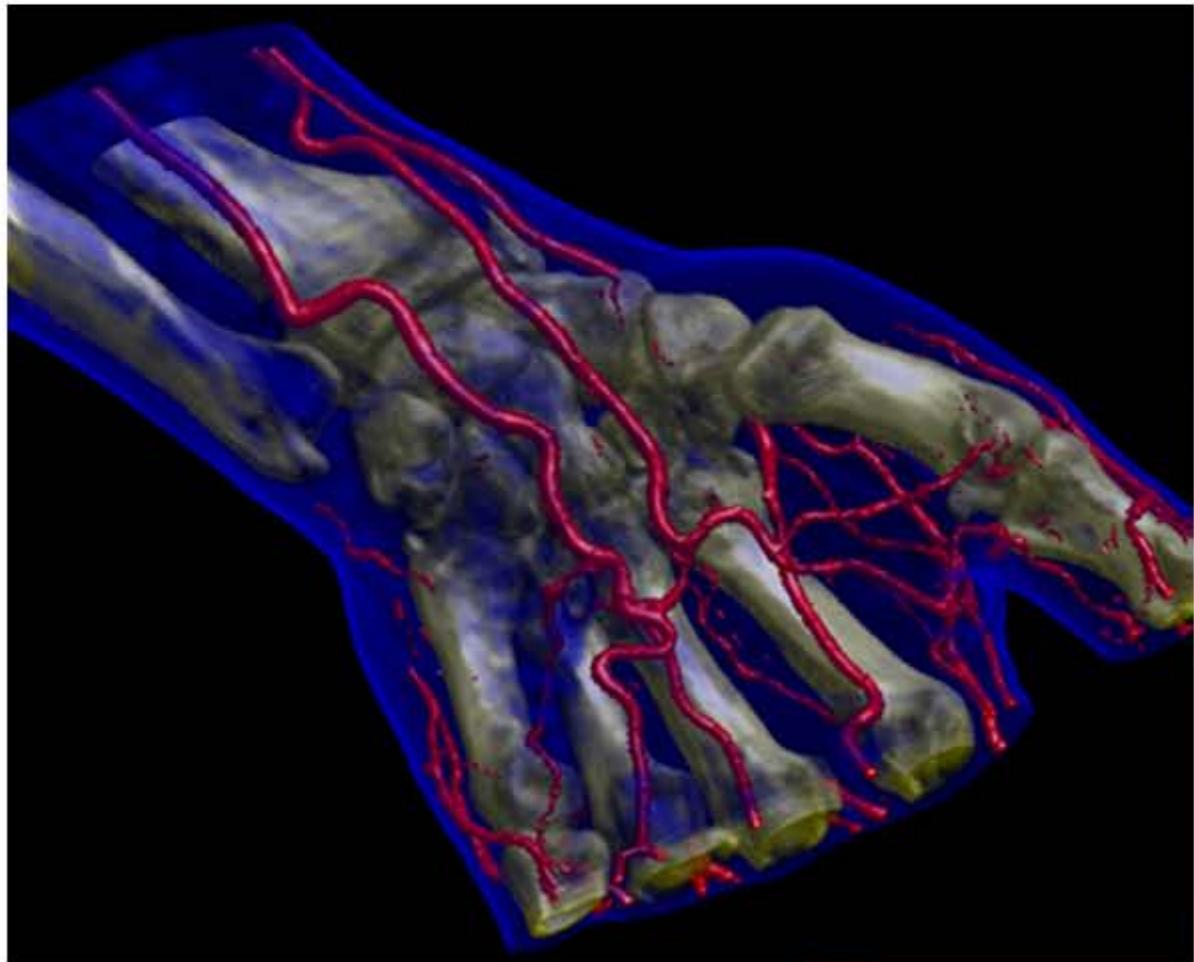
- Gradient magnitude window is main parameter
- Exponent between 4 and 16 is good choice



# Volumetric Boundary Contours (3)

Apply to specific segmented objects

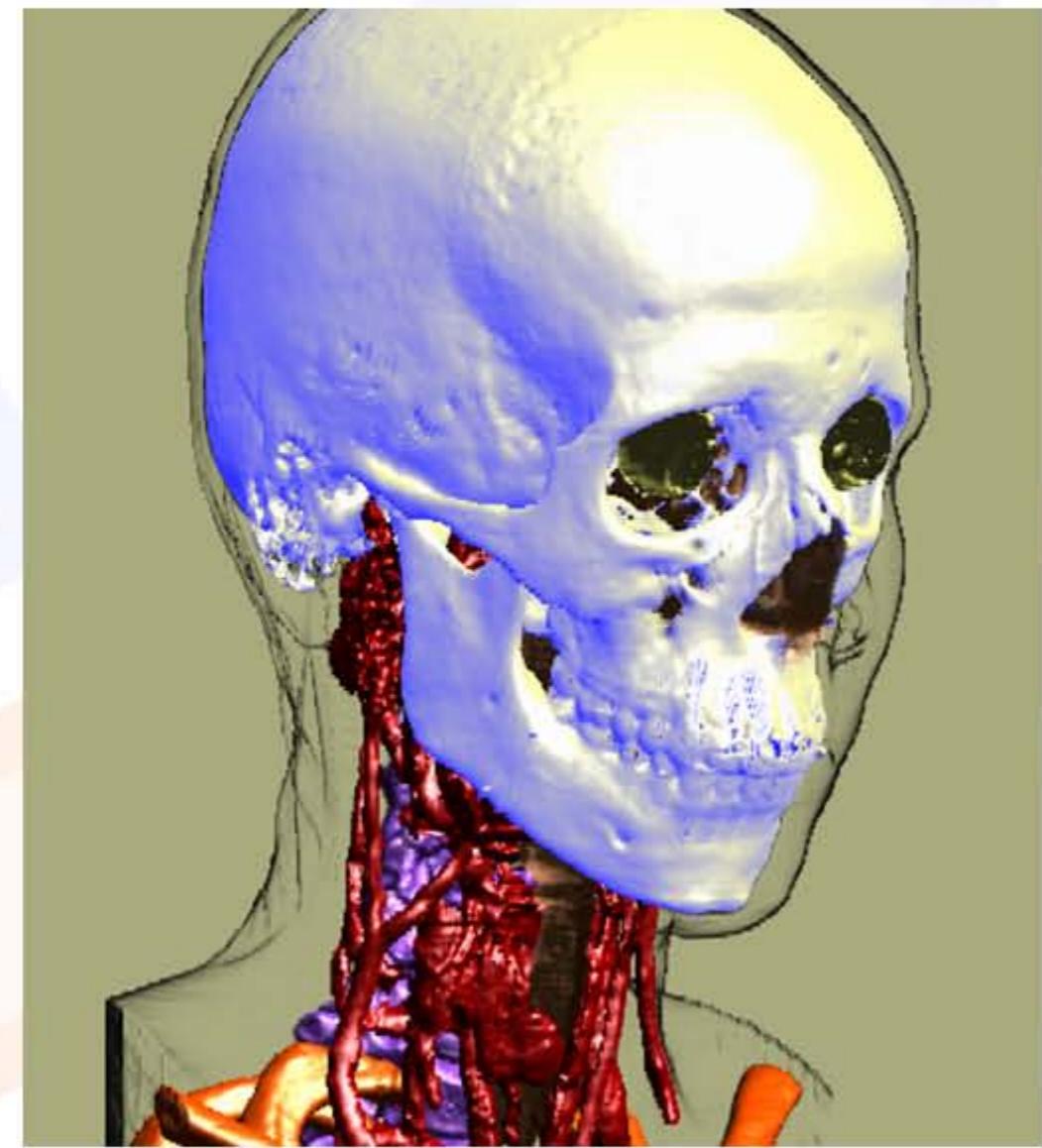
- Provides view-dependent context
- No obstruction of interior



# Volumetric Boundary Contours (3)

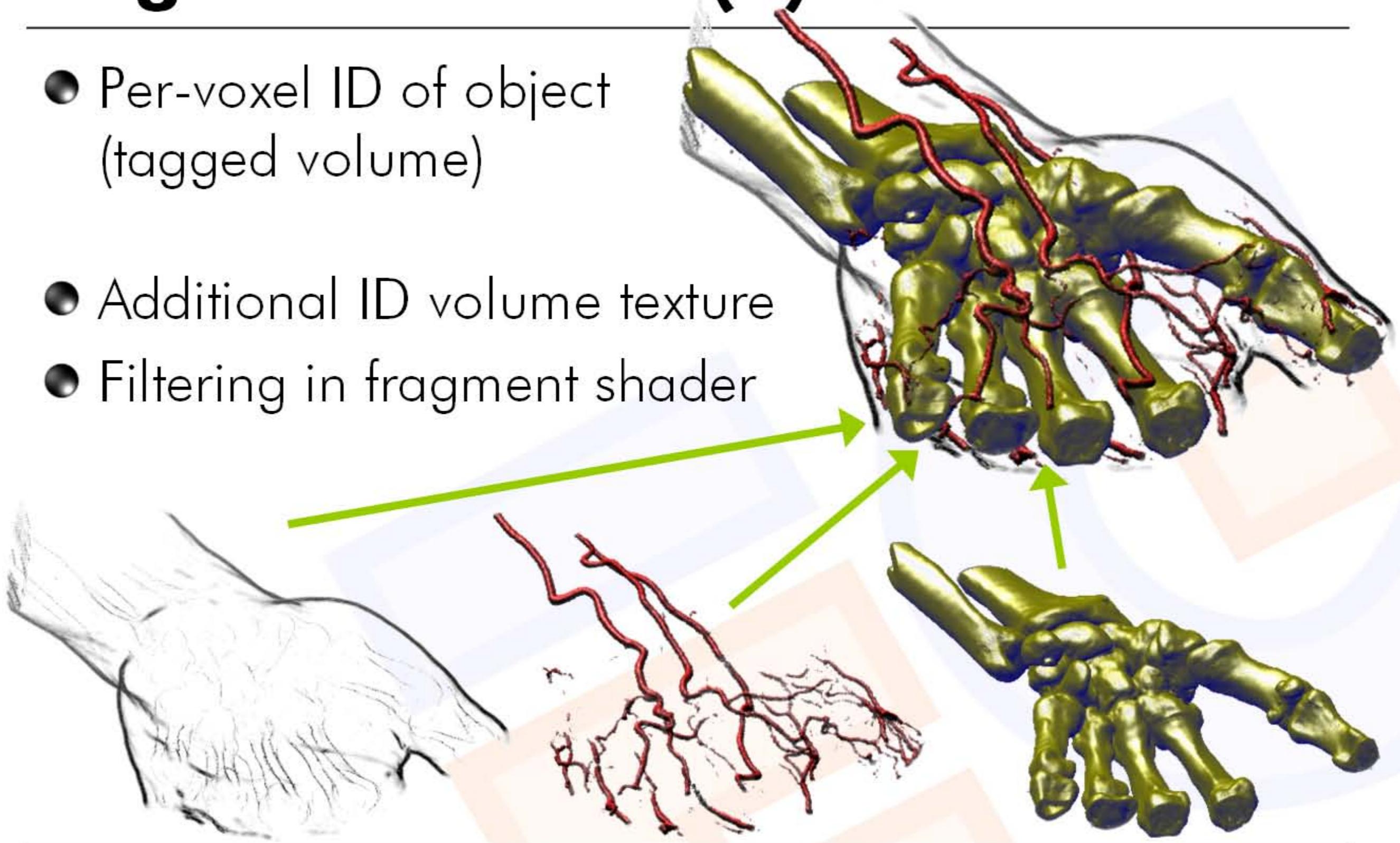
Apply to specific segmented objects

- Provides view-dependent context
- No obstruction of interior



# Segmented Data (1)

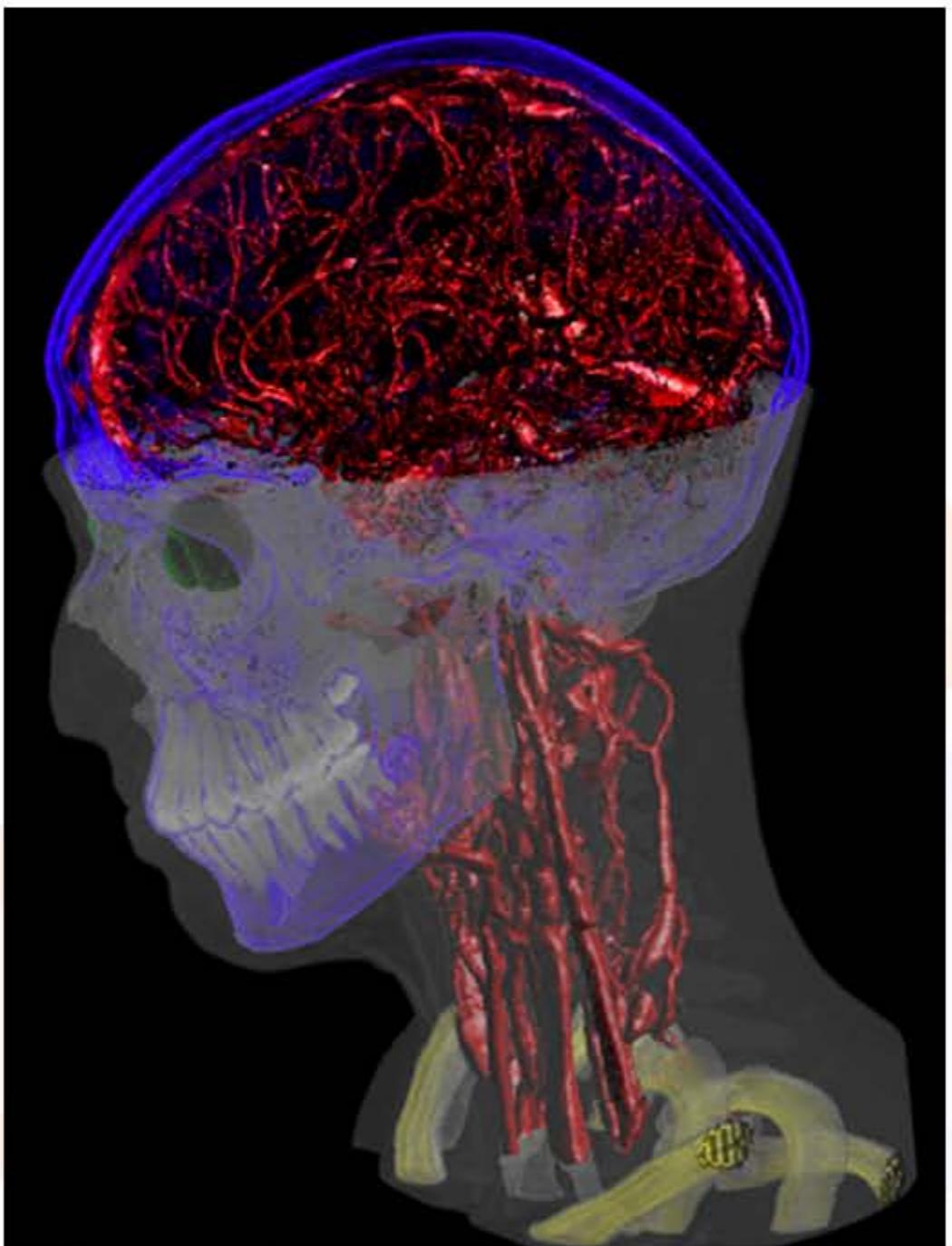
- Per-voxel ID of object  
(tagged volume)
- Additional ID volume texture
- Filtering in fragment shader



# Segmented Data (2)

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- Volumetric boundary contours
- Segmented volumes
  - Focus and context
  - Per-object transfer function
  - Per-object rendering mode
  - Two-level volume rendering



# Curvature Motivation (1)

- Tri-cubic filtering
- Higher-order surface properties
- Curvature visualization
- Non-photorealistic rendering based on curvature



# Curvature Motivation (2)

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- Accessibility shading
- Flow in curvature direction



# Signed Distance Fields

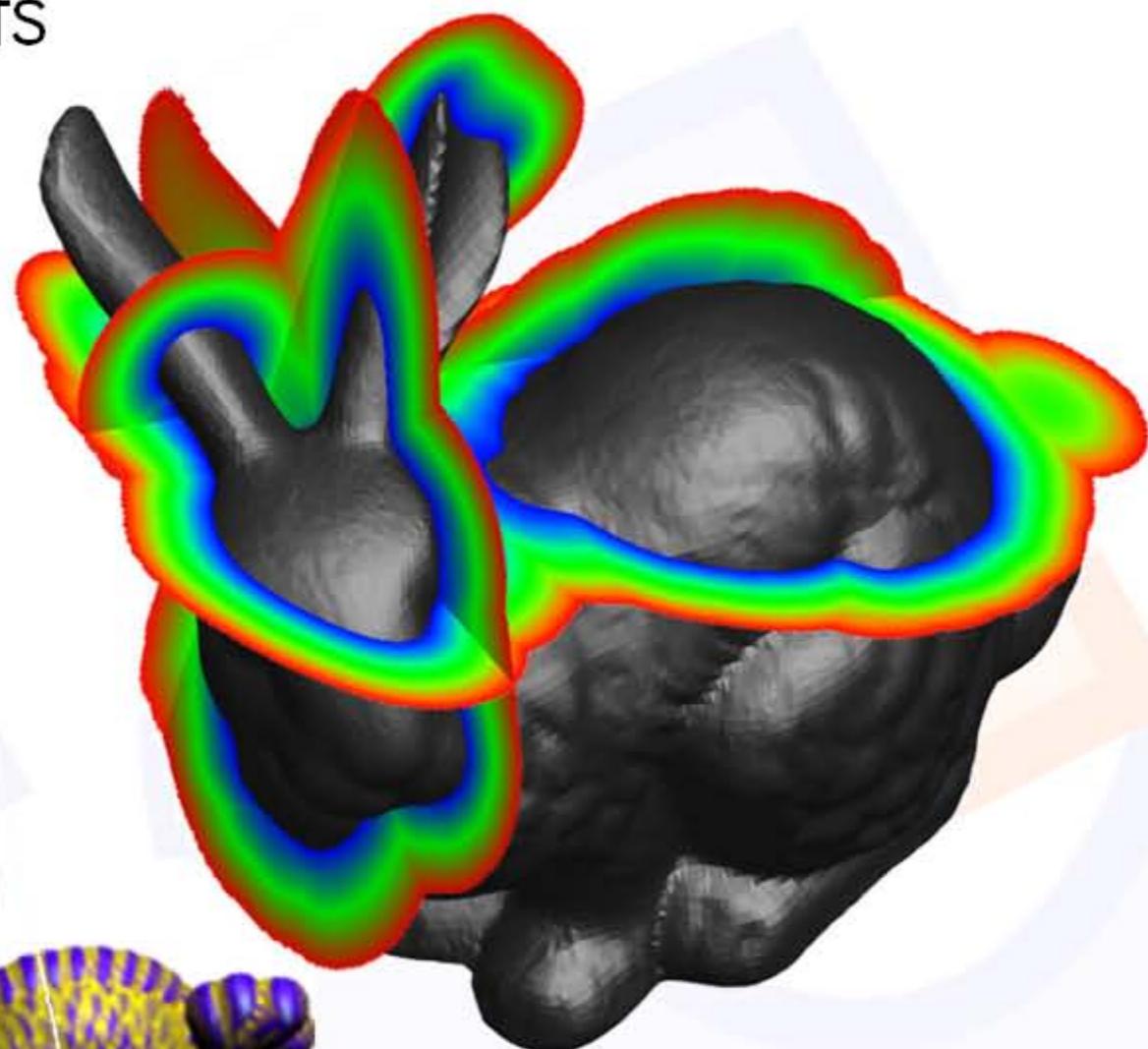
Volume / scalar field for “objects”

- Signed distance to surface

$$\phi : \mathbb{R}^3 \mapsto \mathbb{R}$$

- Implicit surface: zero level set

$$S = \{\mathbf{x} | \phi(\mathbf{x}) = 0\}$$



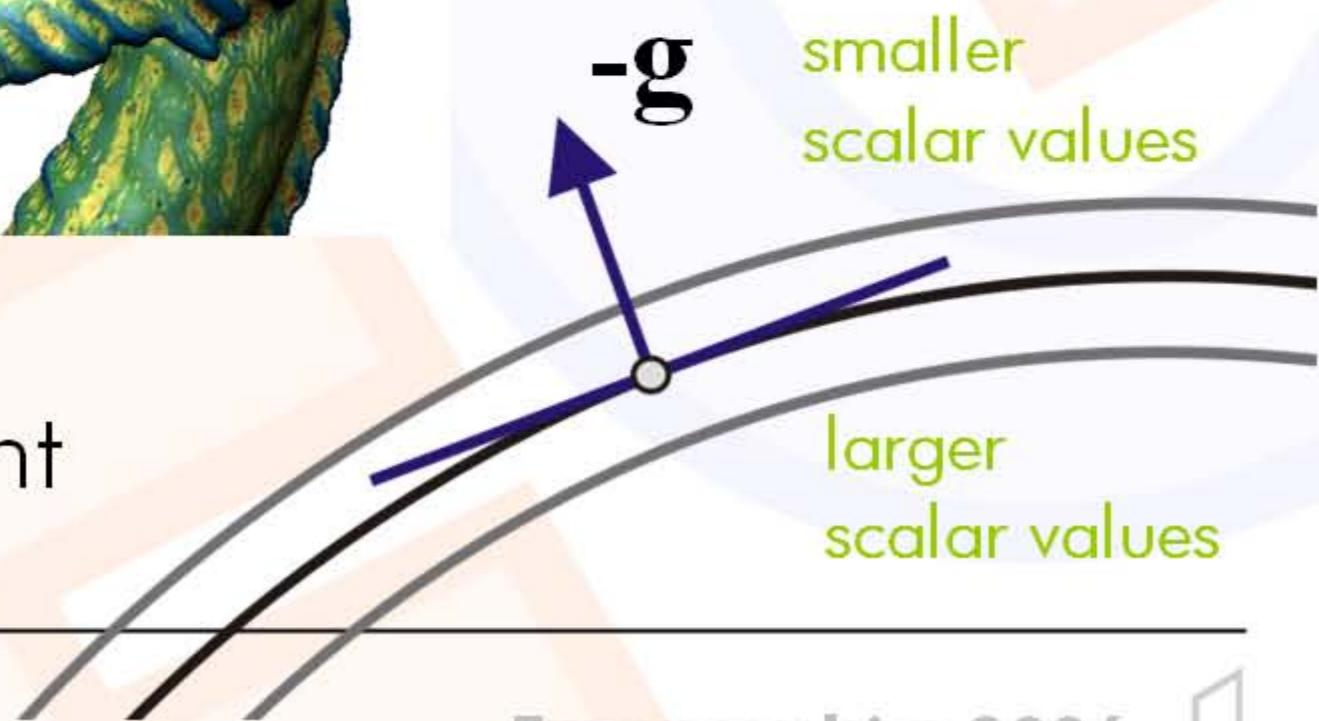
# Curvature-Based Isosurface Illustration

- Curvature measure color mapping
- Curvature directions; ridges and valleys



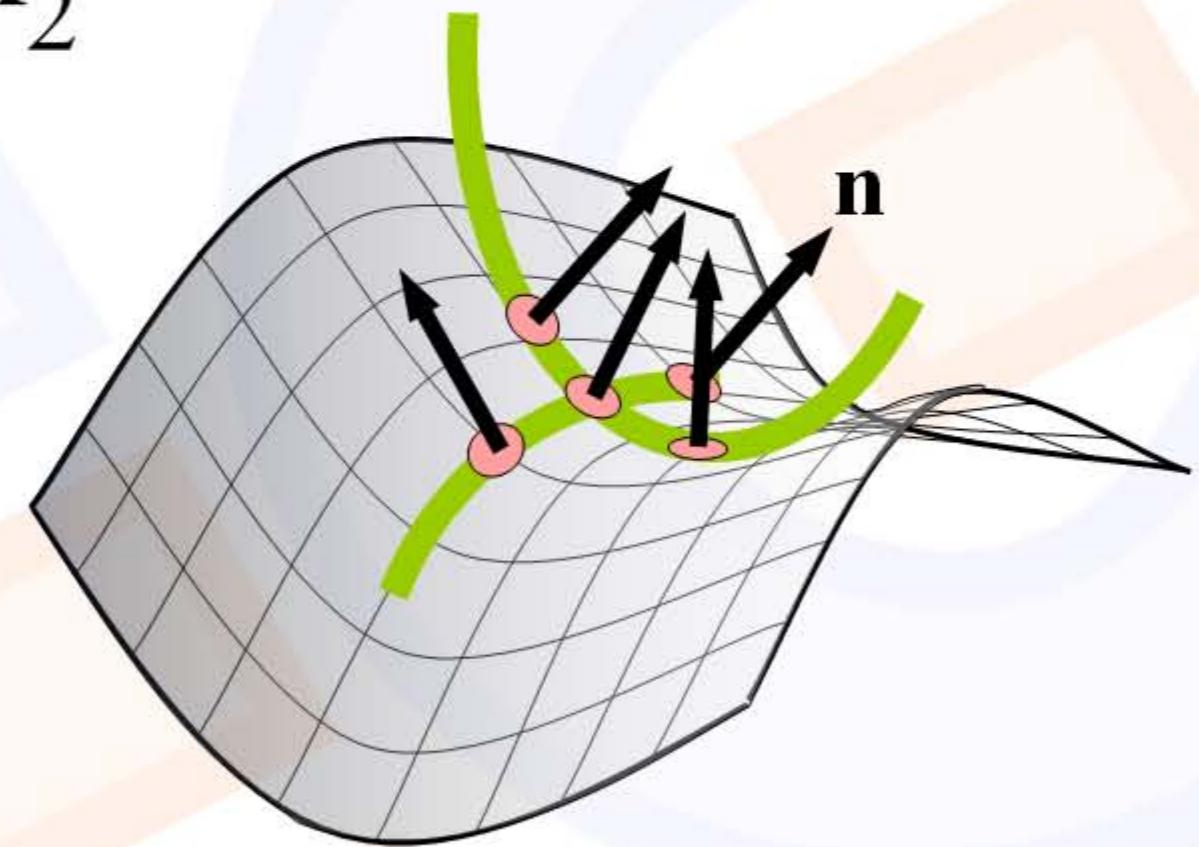
Implicit surface curvature

- Isosurface through a point



# Curvature

- How do small positional changes on the surface change the normal vector? “derivative” of normal
- First and second principal curvature:  
maximum:  $K_1$  minimum:  $K_2$



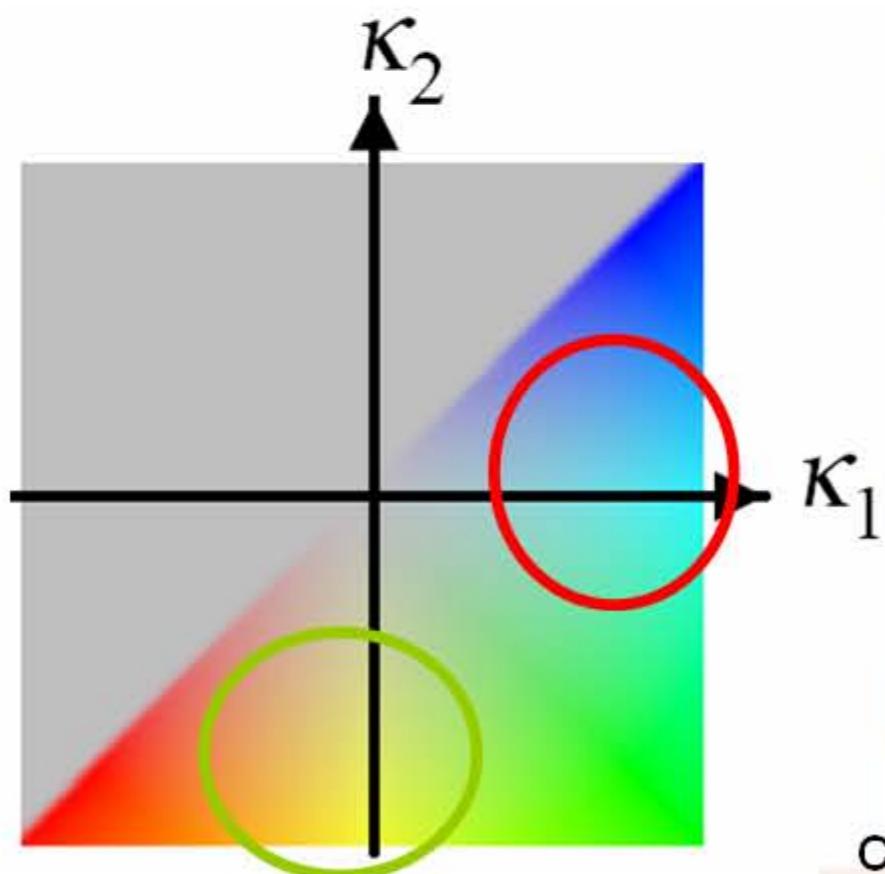
- Curvature directions
- Curvature magnitudes

courtesy of Gordon Kindlmann

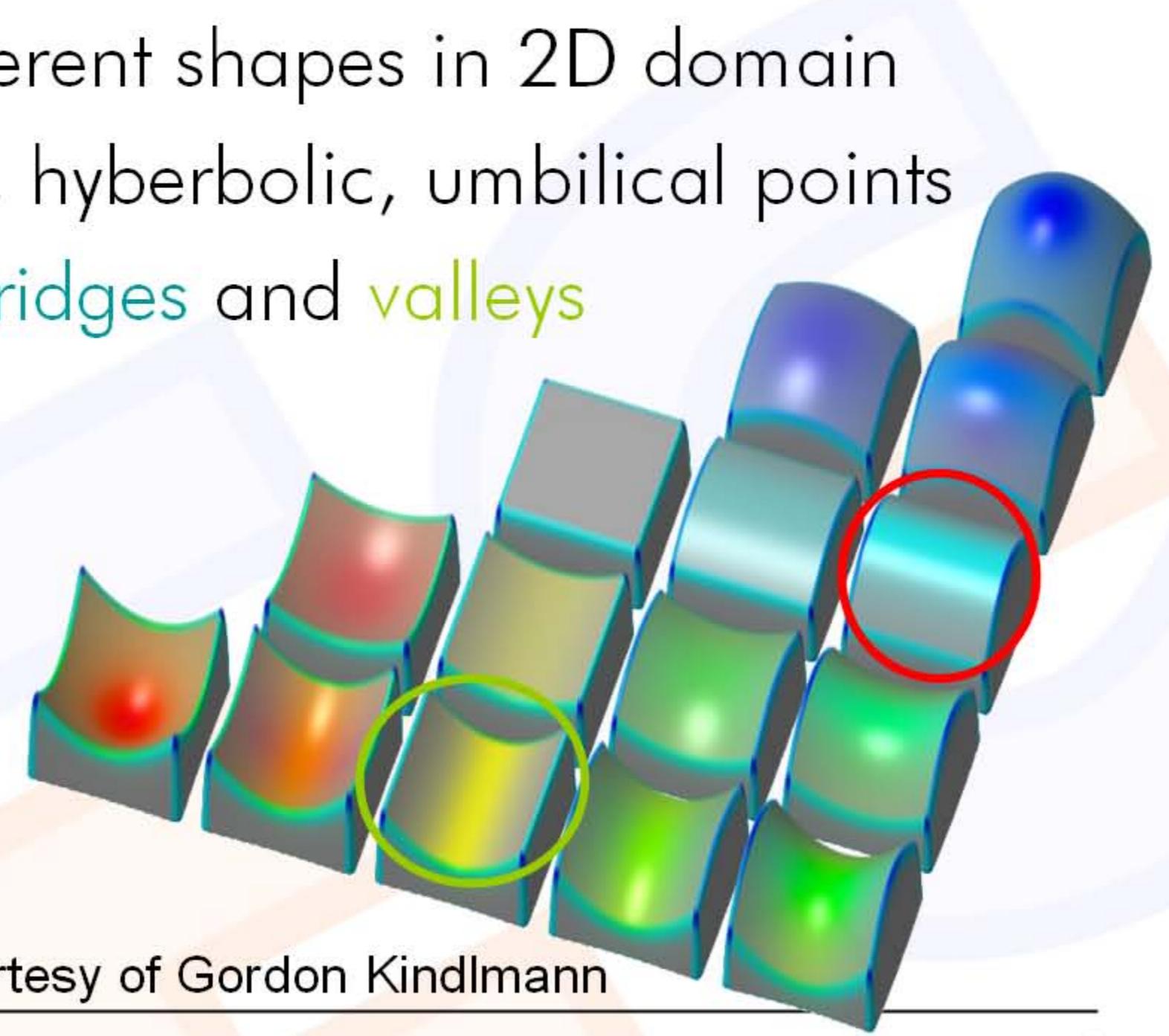
# The Principal Curvature Domain

Maximum/minimum principal curvature magnitude

- Identification of different shapes in 2D domain
- Elliptical, parabolic, hyperbolic, umbilical points
- Feature lines: e.g., ridges and valleys

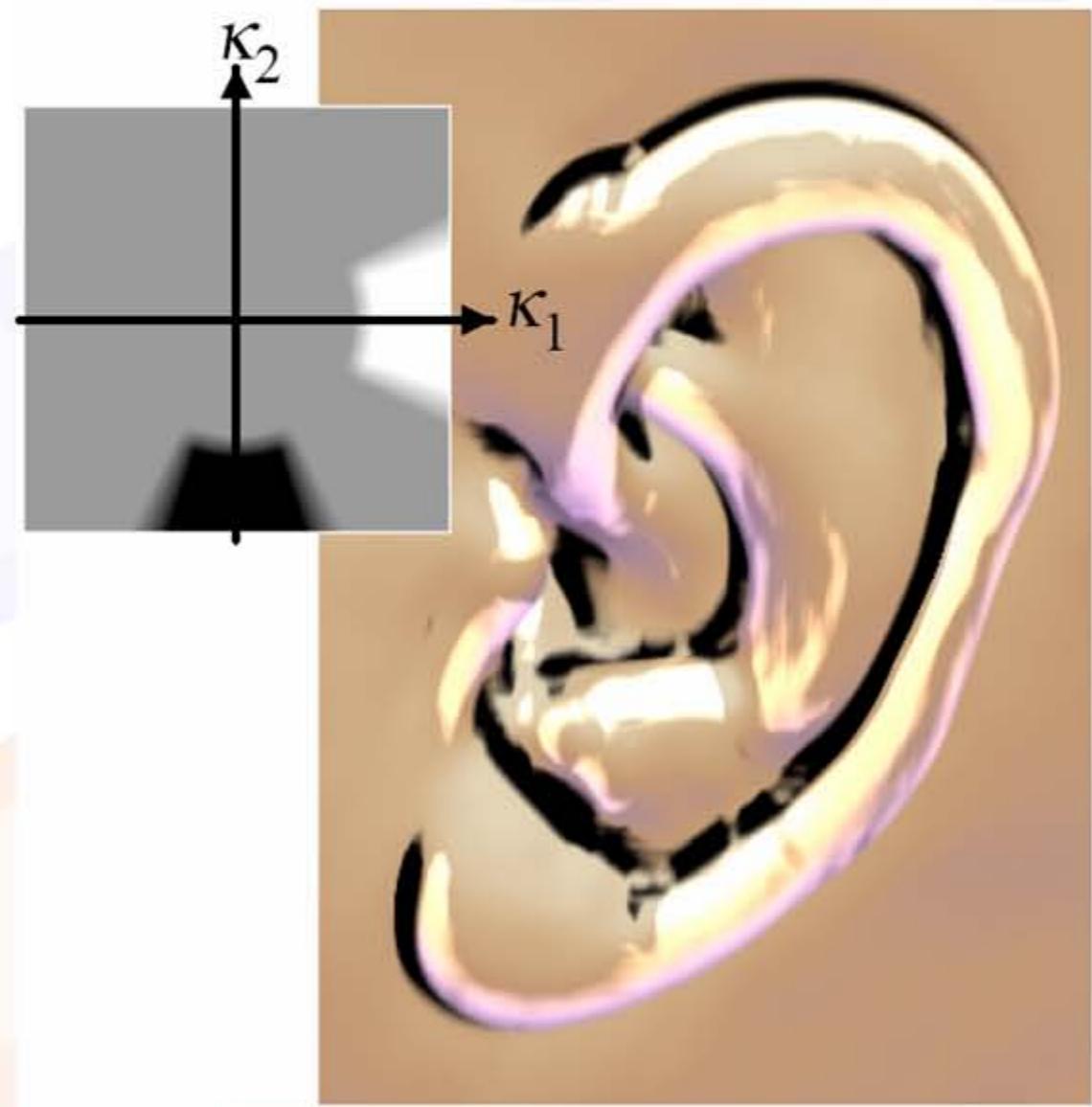
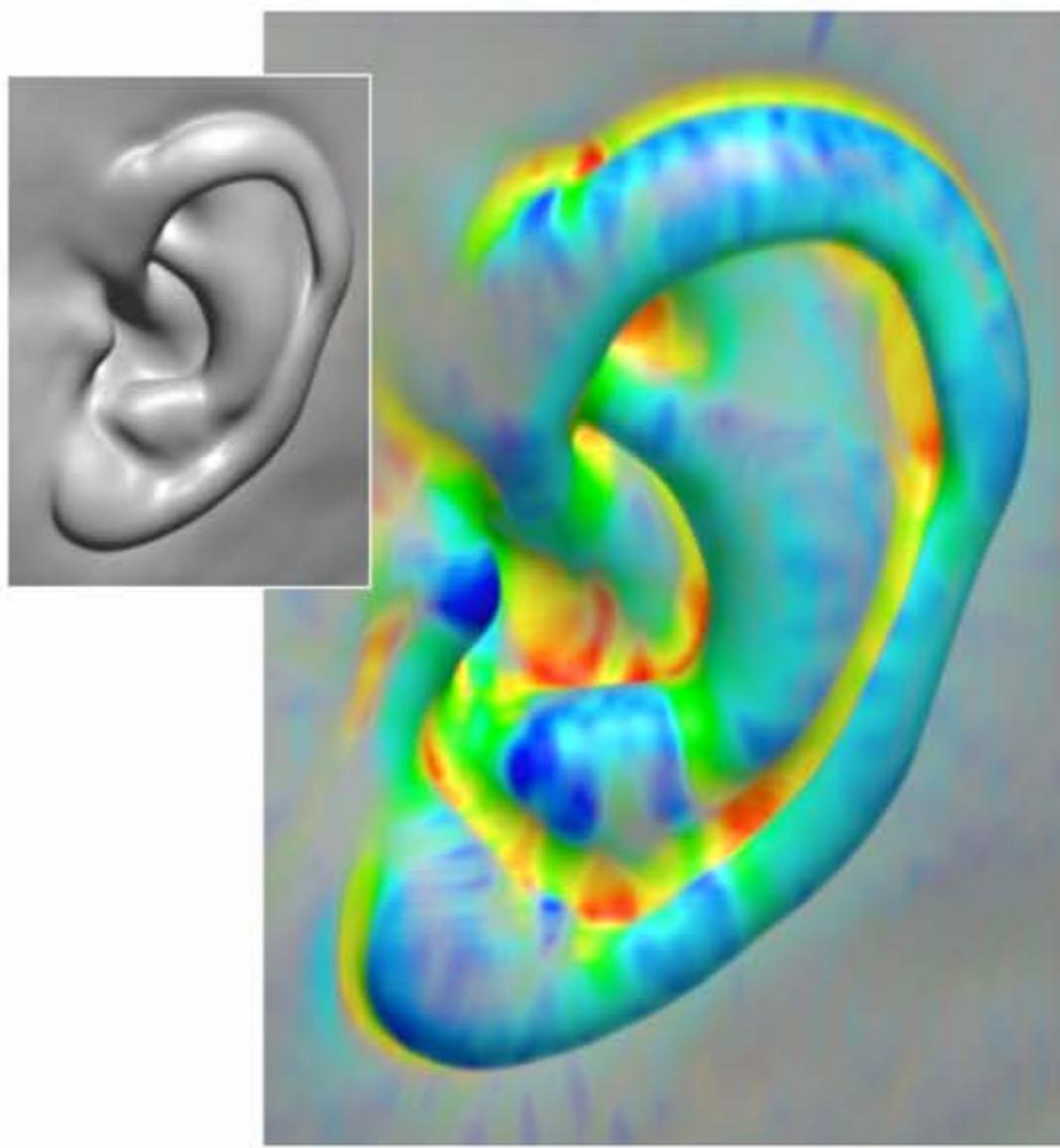


courtesy of Gordon Kindlmann



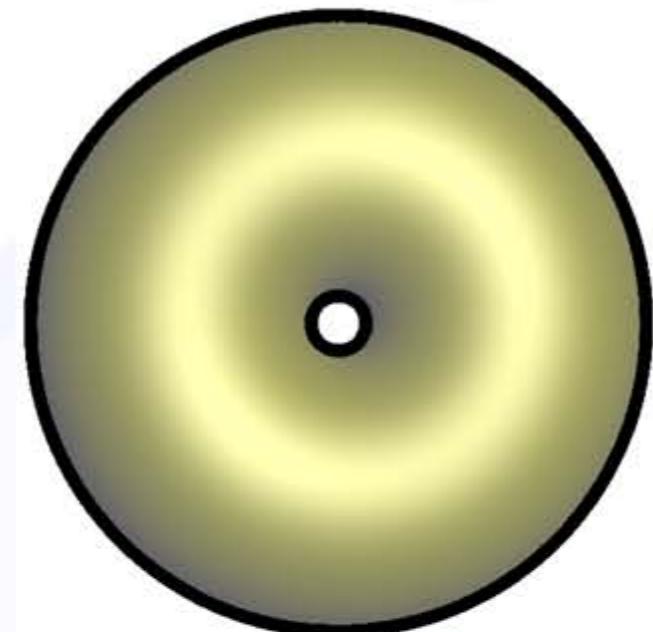
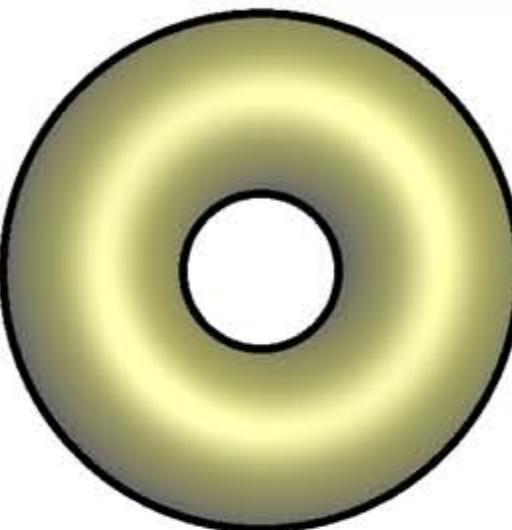
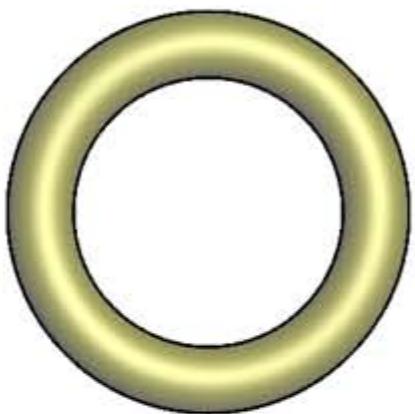
# Curvature Transfer Functions

- Color coding of curvature domain
- Paint features: ridge and valley lines

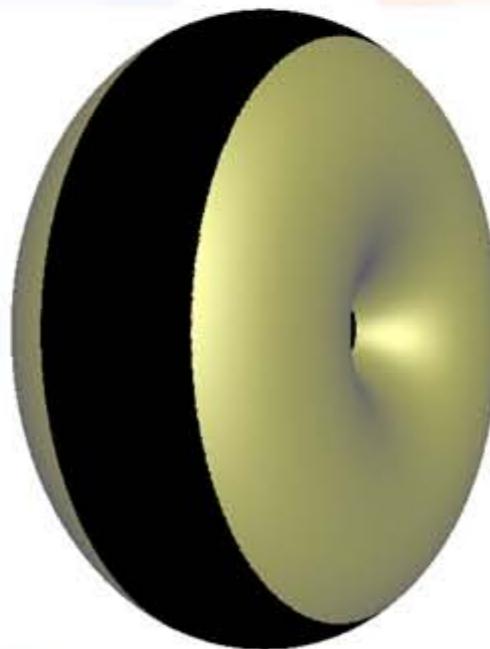
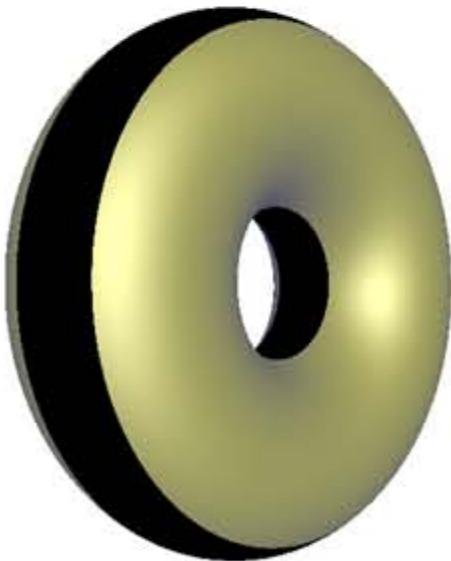


# Problems of Implicit Surface Contours

- Constant threshold on  $|\mathbf{v} \cdot \mathbf{n}|$

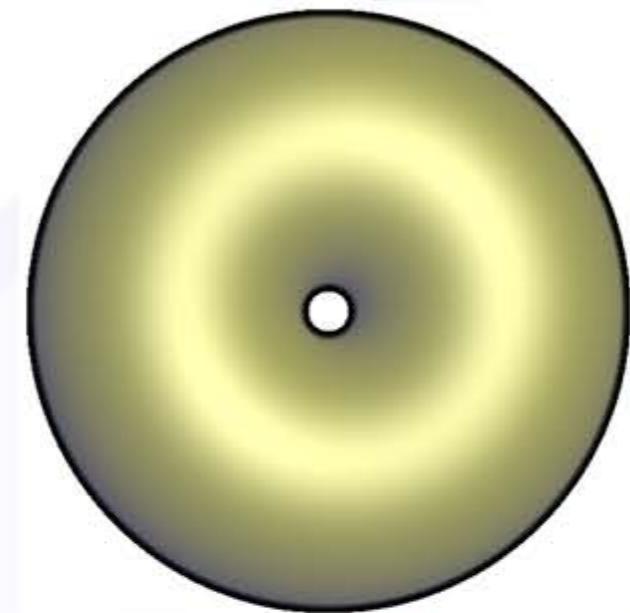
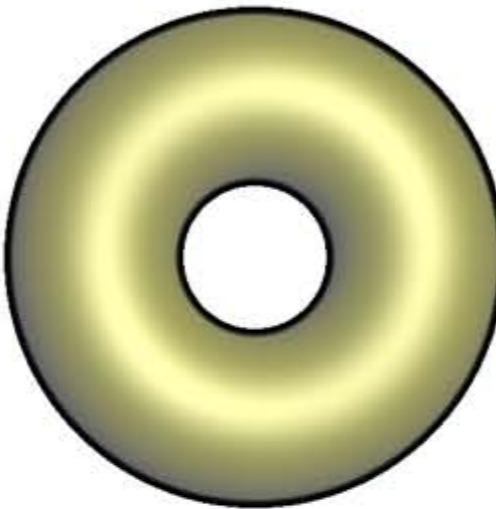
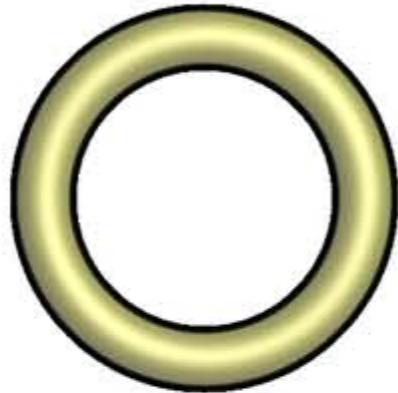


- Thickness changes!

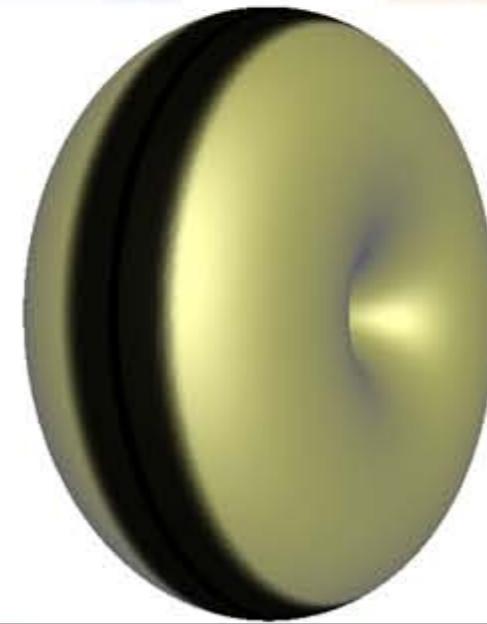
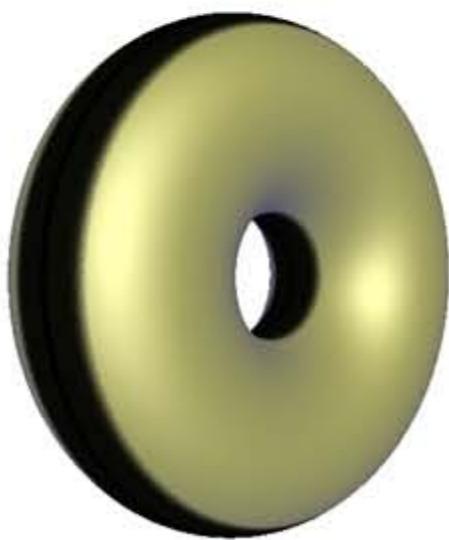


# Curvature-Based Contour Threshold (1)

- Threshold dependent on curvature in view direction



- Thickness constant!



# Curvature-Based Contour Threshold (2)

- Higher curvature in view direction needs higher threshold



# Implicit Curvature via Convolution

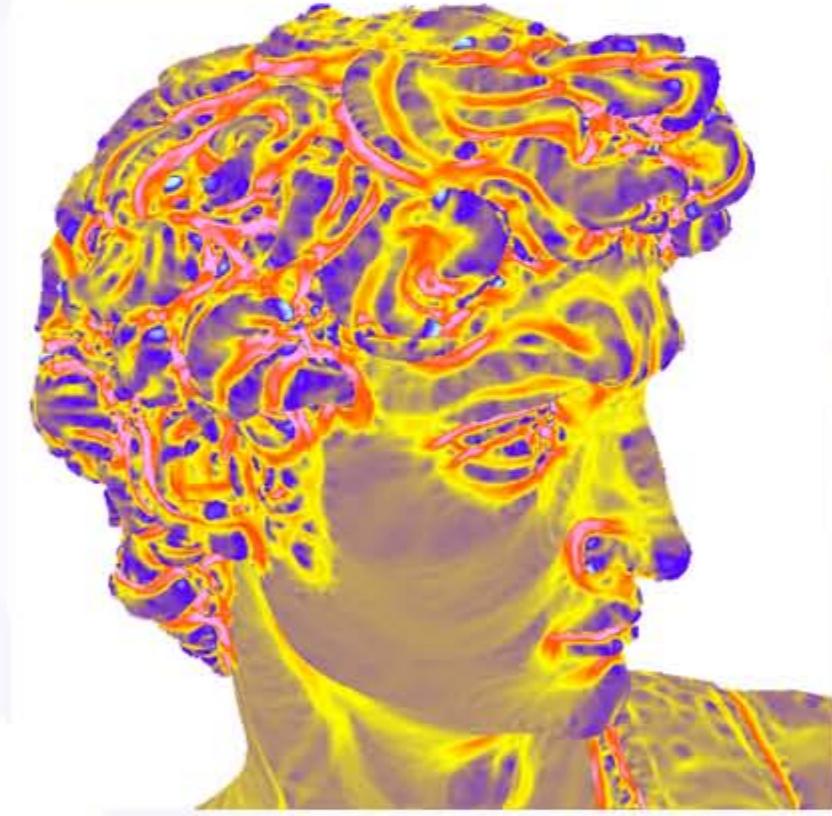
- Computed from first and second derivatives
  - Can use fast texture-based tri-cubic filters in shader
  - Can use **deferred** computation and shading



first derivative



maximum curvature



minimum curvature

# Deferred Isosurface Shading

- Shading is expensive
- Compute surface intersection image from volume
- Compute derivatives and shading in image space



intersection image



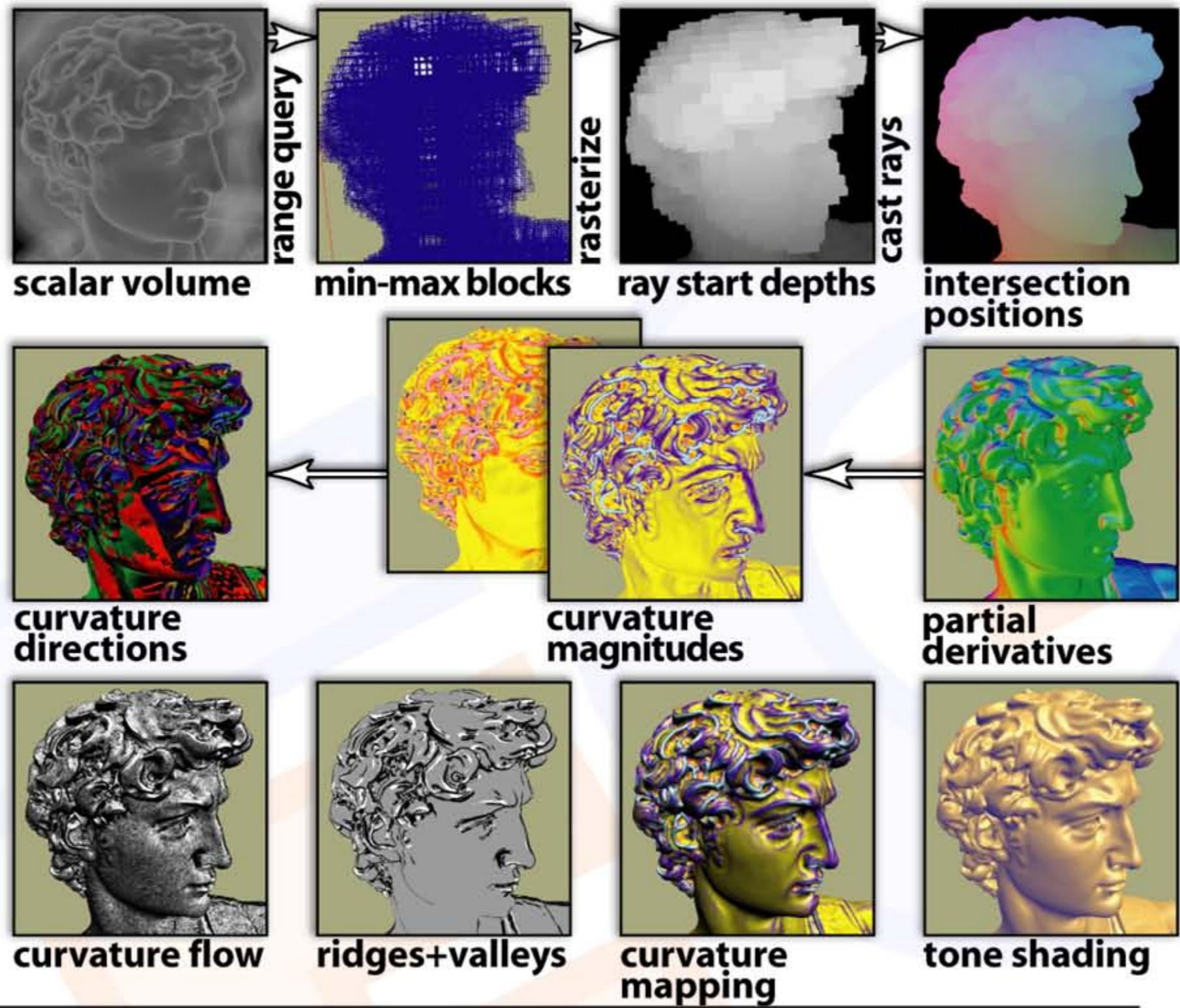
curvature color coding



ridges and valleys

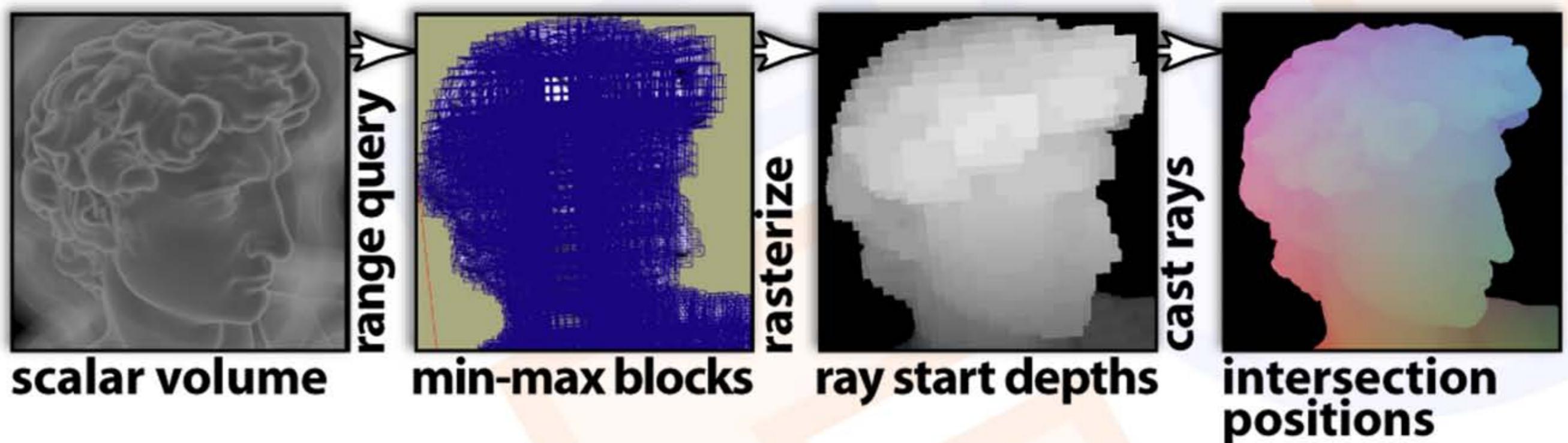
# Pipeline Overview

- Ray-casting
- Differential properties (deferred computation)
- Deferred shading



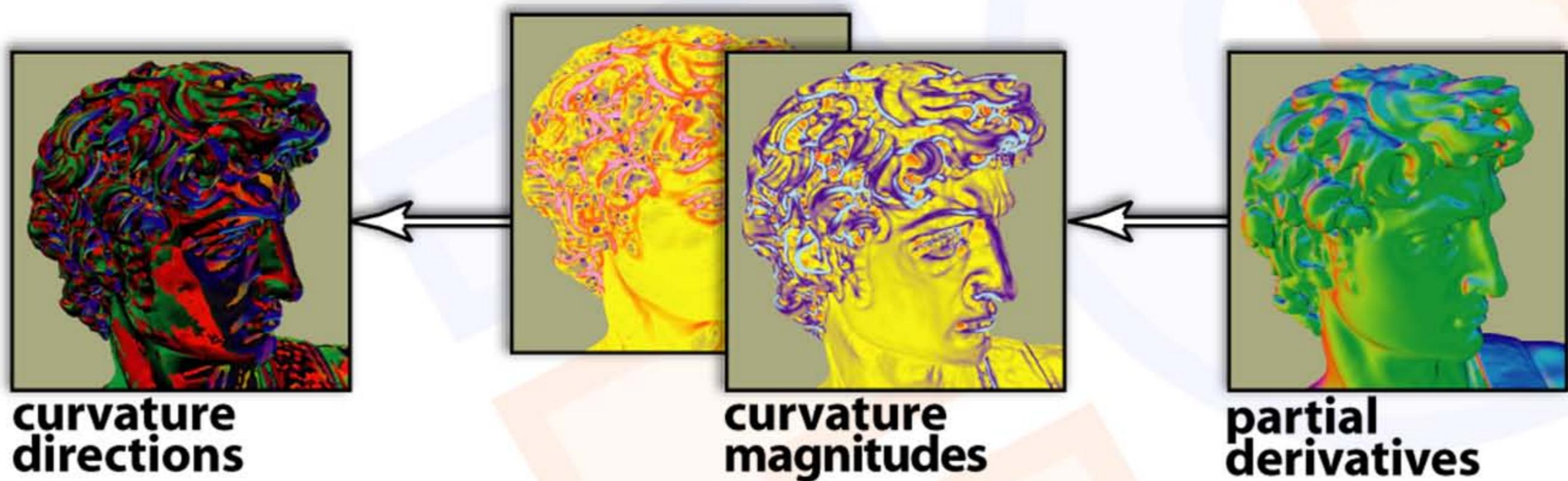
# Pipeline Stage #1: Ray-Casting

- Rasterize faces of active min-max blocks
- Cast into the volume; stop when isosurface hit
- Refine isosurface hit positions (root search)



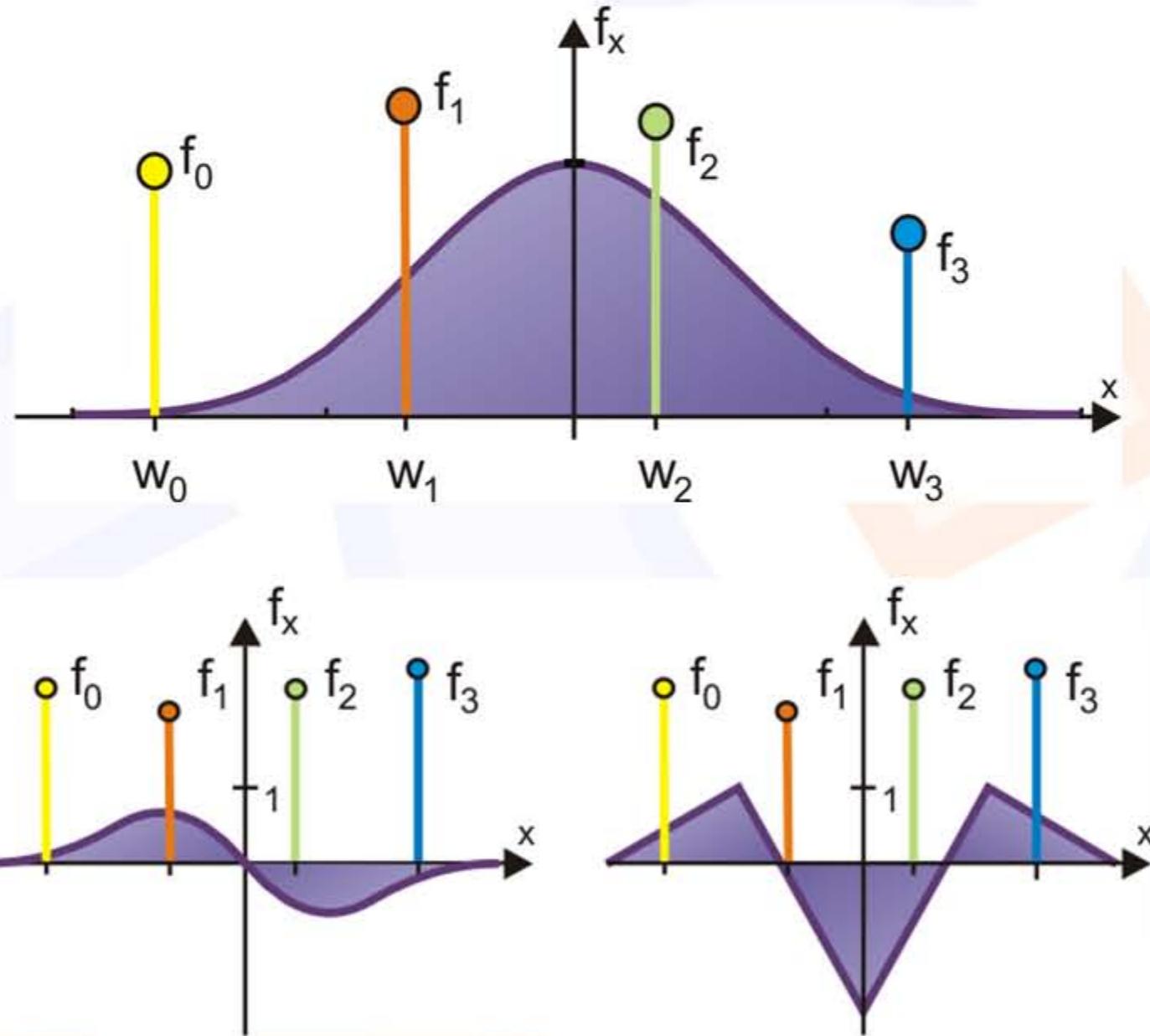
# Pipeline Stage #2: Differential Props.

- Basis for visualization of surface shape
- First and second derivatives (gradient, Hessian)
- From these: curvature information, ...



# Value and Derivative Reconstruction

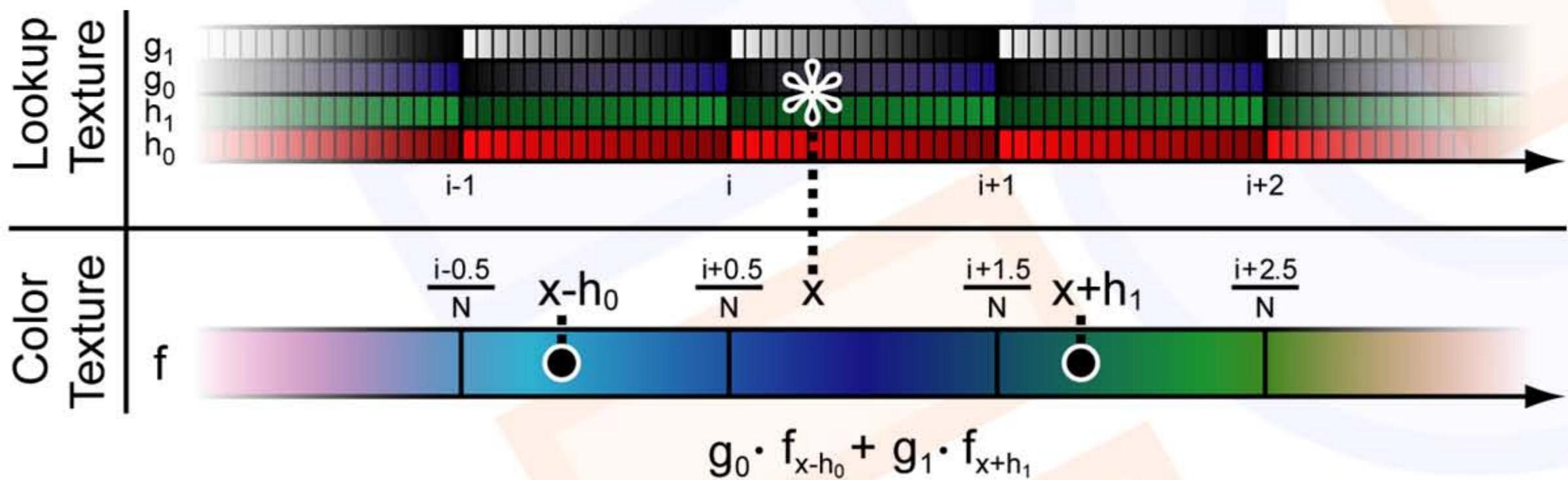
- Cubic B-spline and derivatives
- Use 1D kernels and tensor product for tri-cubic filtering
- Well-suited for curvature computation  
[Kindlmann et al., 2003]
- Expensive convolution?



# Fast Tri-Cubic Filtering on GPUs

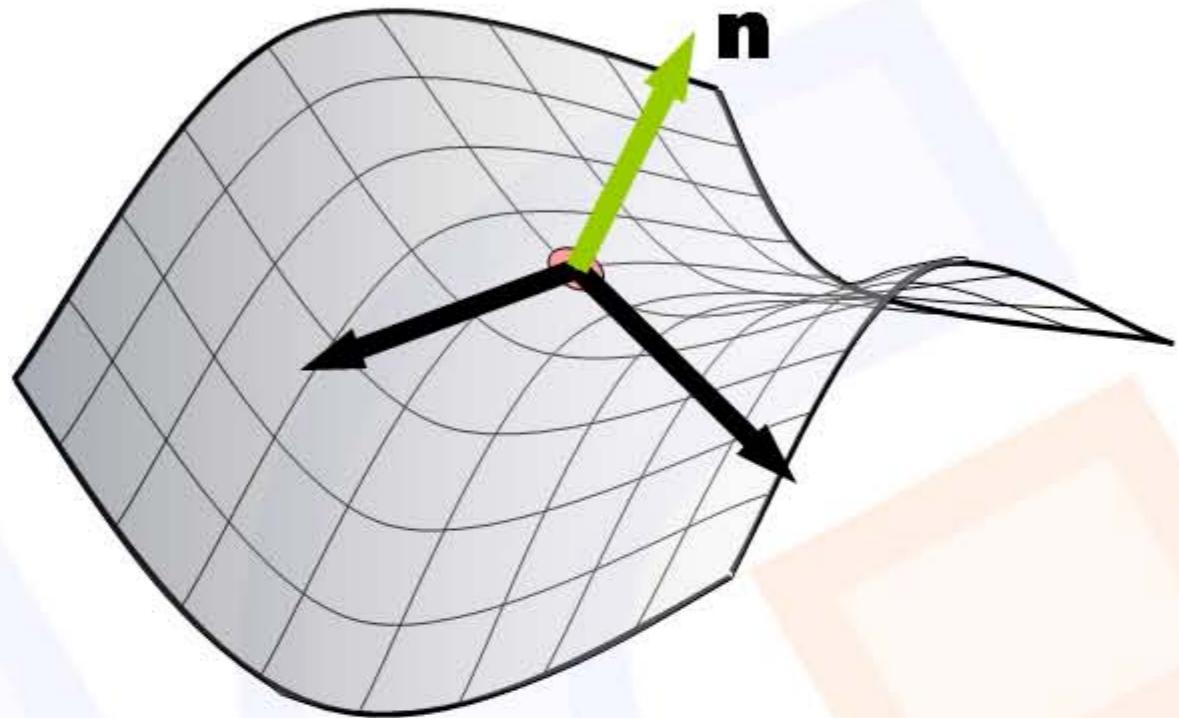
- Usually 64 nearest-neighbor lookups
- But 8 tri-linear lookups suffice for tri-cubic B-spline
- Kernels are transformed into 1D textures

[Sigg and Hadwiger, GPU Gems 2, 2005]



# Curvature Computation

- Build on gradient and Hessian matrix
- Hessian contains curvature information
- Transform Hessian into tangent space
- Curvature magnitudes: eigenvalues of  $2 \times 2$  matrix
- Curvature directions: eigenvectors of  $2 \times 2$  matrix



# Pipeline Stage #3: Shading

- Build on previous images
  - Position in volume space
  - Gradient
  - Principal curvature magnitudes and directions



**curvature flow**



**ridges+valleys**



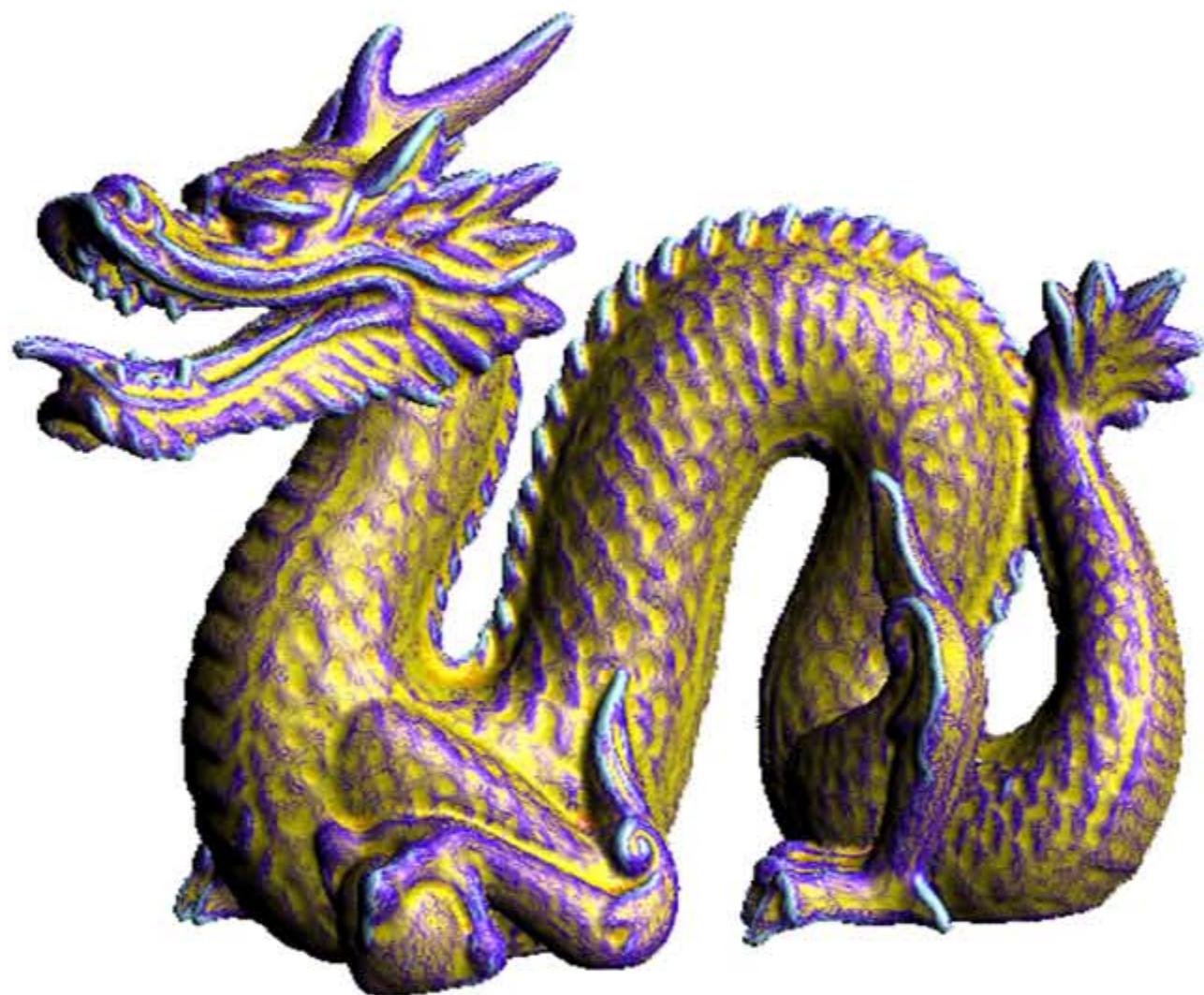
**curvature  
mapping**



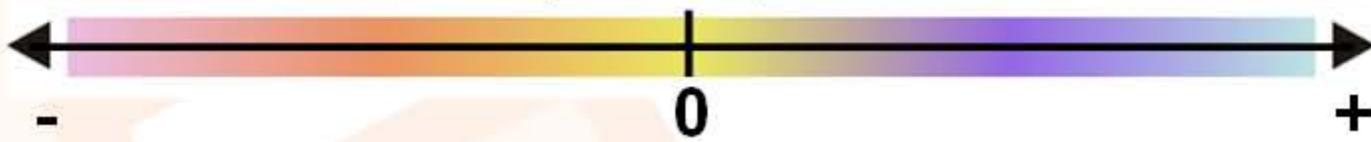
**tone shading**

# Color Coding Scalar Curv. Measures

- 1D color lookup table

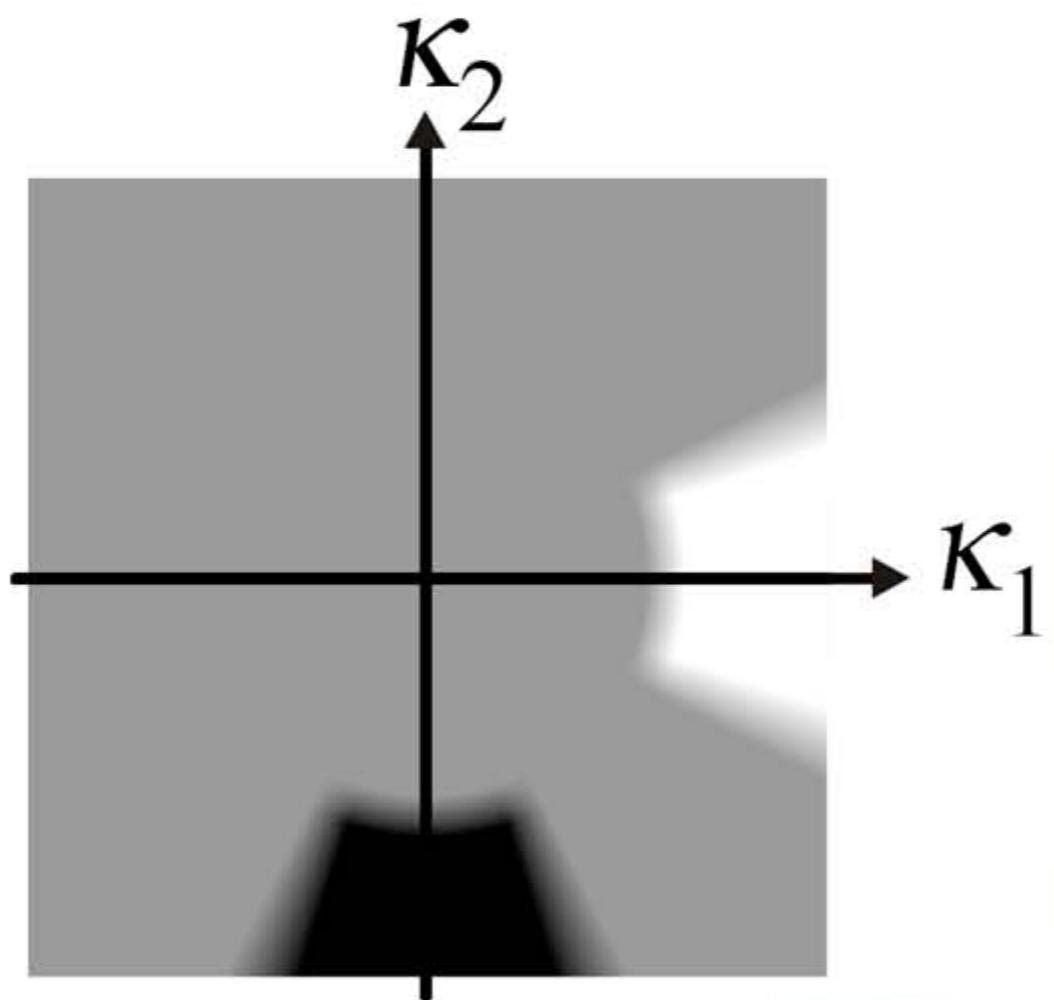


maximum principal curvature



# 2D Curvature Transfer Functions

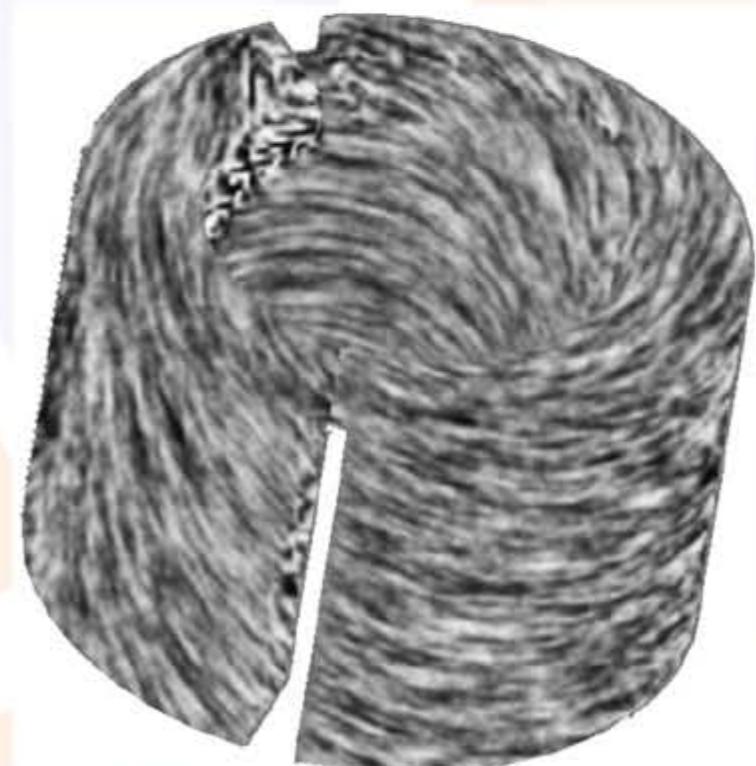
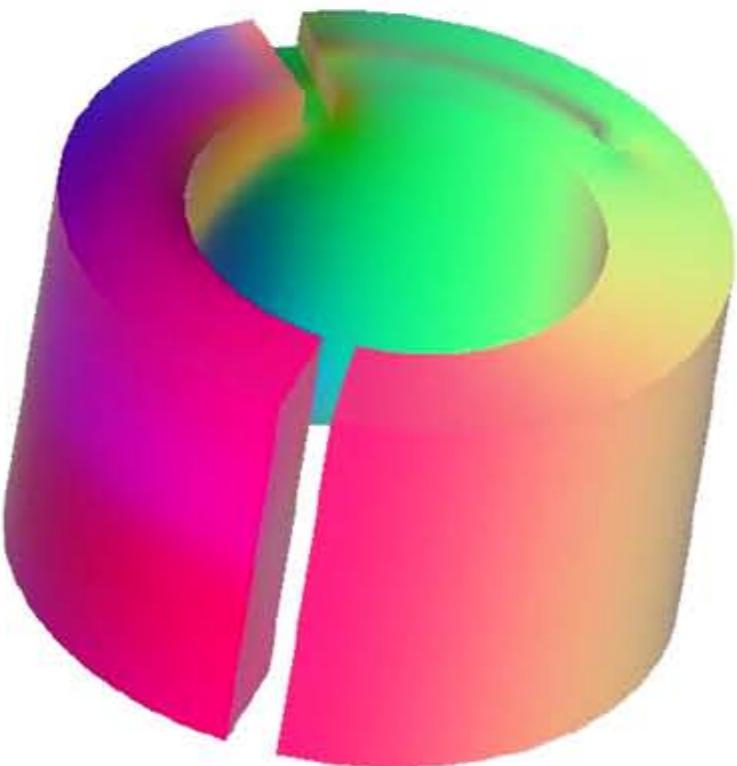
- 2D lookup table in domain of principal curvatures



ridges and valleys, plus contours:

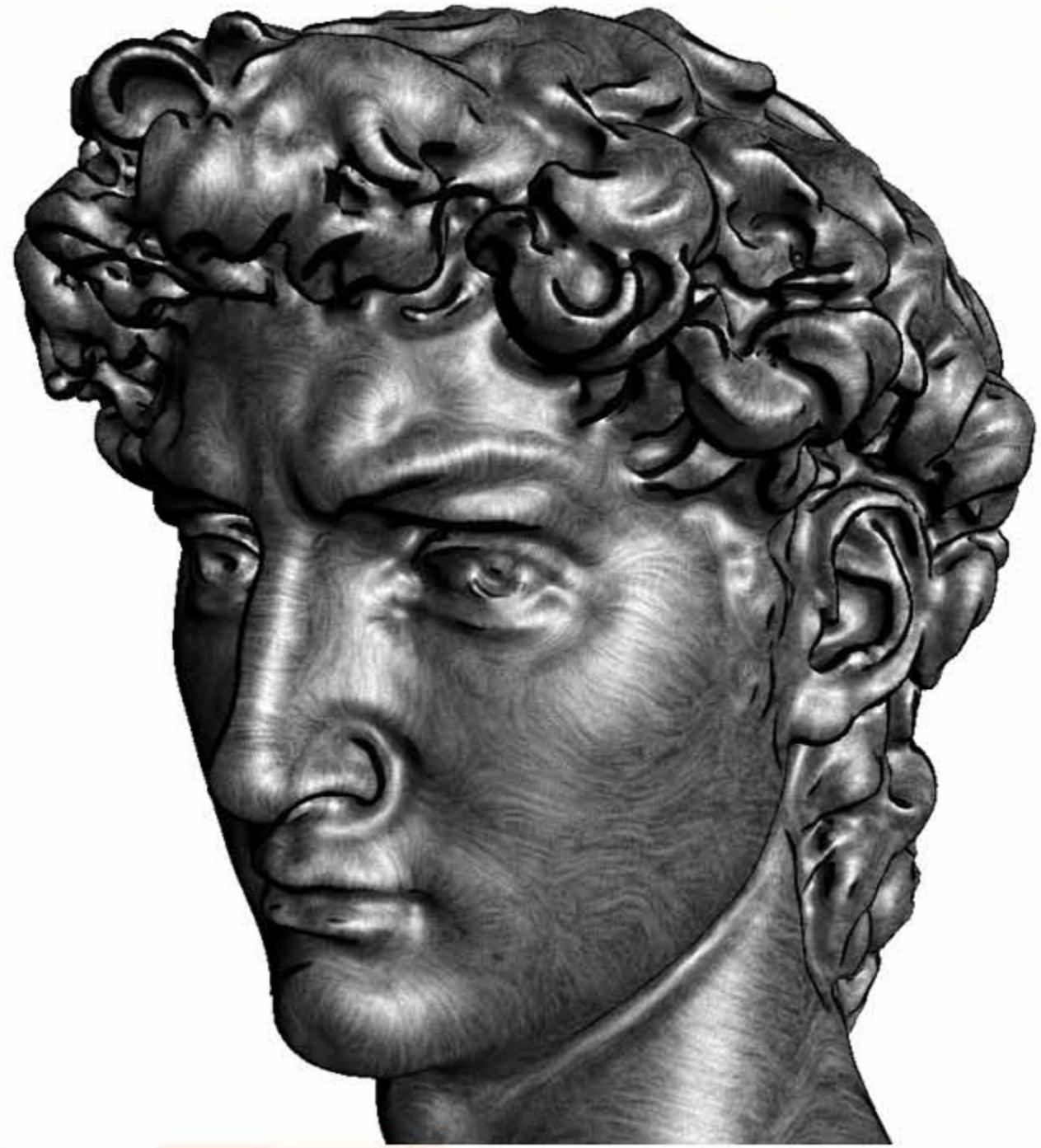
# Visualizing Curvature Directions (1)

- Use 3D vector field visualization on curved surfaces  
[van Wijk, Vis 2003], [Laramée et al., Vis 2003]
- Project 3D vectors to screen space
- Advect dense noise textures in screen space



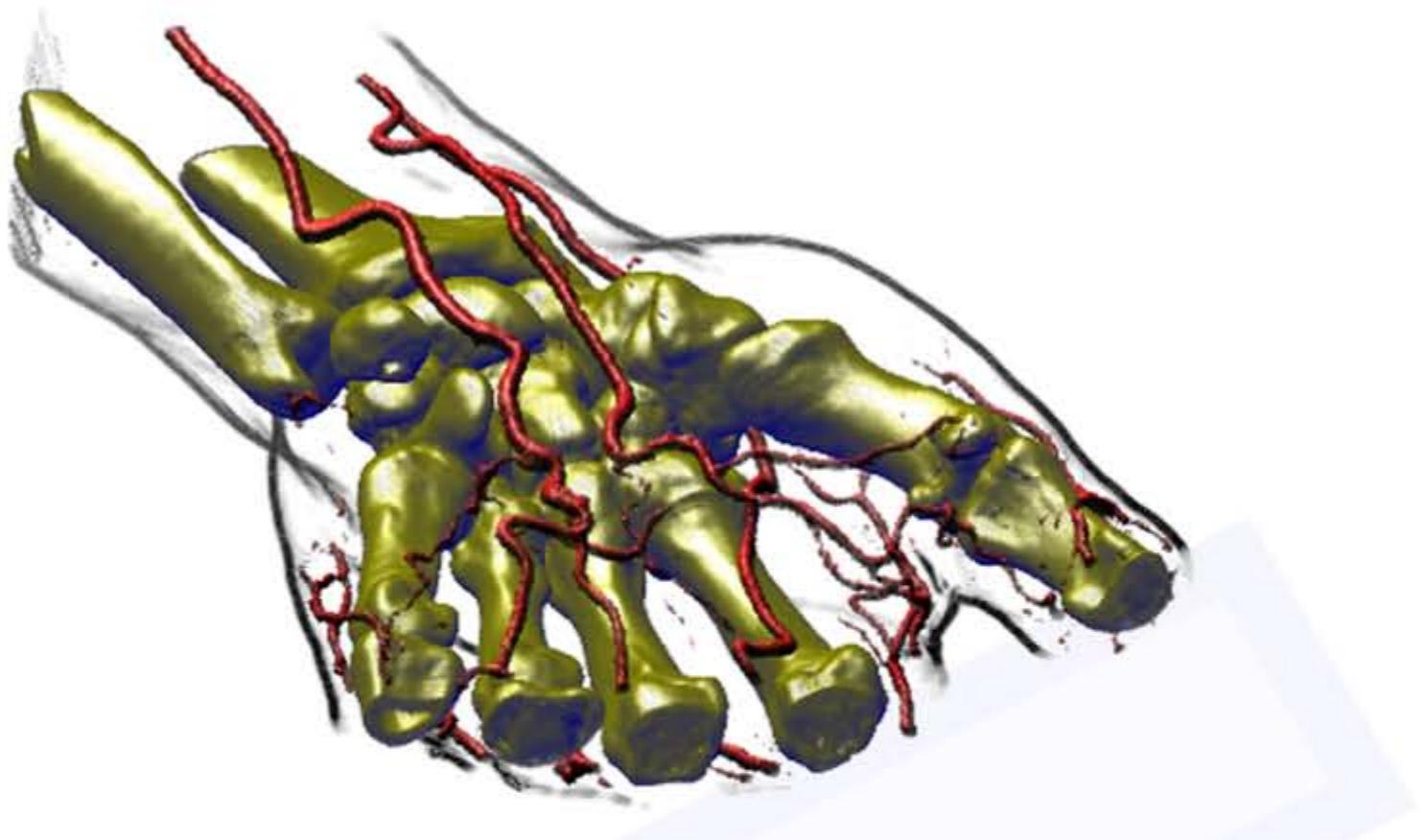
# Visualizing Curvature Directions (2)

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# Thank You!

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## Acknowledgments

- Gordon Kindlmann, Christian Sigg,  
Henning Scharsach, Bob Laramee, Jiri Hladuvka
- VRVis is funded by the Kplus program of the Austrian government