

The image part with relationship ID r553 was not found in the file.

# Deep Learning for Computational Imaging

Birsen Yazıcı

*Bariscan Yonel, Eric Mason\*, Samia Kazemi*

Department of Electrical, Computer and Systems Engineering

Rensselaer Polytechnic Institute

\*Tactical Electronic Warfare Division, Naval Research Laboratory,  
Washington, DC

April 12<sup>th</sup>, 2019

# Background

---

- Professor of Electrical Computer and System Engineering at Rensselaer Polytechnic Institute, Troy, NY

## Research Interests

- Applied mathematics
- Statistical signal processing, machine learning, optimization
- Wave-based imaging, inverse scattering & tomography
  - Radar, sonar, diffuse optical imaging

# Computational Imaging Laboratory at RPI

---

- Prof. Birsen Yazıcı
- Supervised 12 PhD thesis, 8 MS thesis
- Dr. Il-Young Son, post-doc
- PhD students
  - Bariscan Yonel
  - Samia Kazemi
  - Sean Thammakoune
  - Airas Akhtar
- MS students
  - Ziya Su
  - Jianyu Yang

# Outline

---

- Fundamentals of Deep Learning
  - Basic concepts and ideas in Deep Learning
  - Traditional machine learning vs Deep Learning
  - Advantages and problems of Deep Learning
- Deep Learning for Inverse Problems in Imaging
- Deep Learning based for Synthetic Aperture Imaging
  - Passive SAR Imaging
  - ATR-aware Synthetic Aperture Imaging
- Conclusion

# Why Deep Learning?

---

- Staggering performance in difficult classification tasks

- Abundance of data
- Minimal upfront engineering
- Fundamental connections to iterative processes, optimization and Bayesian decision making
- A framework to combine modeling and data synergistically

# Outline

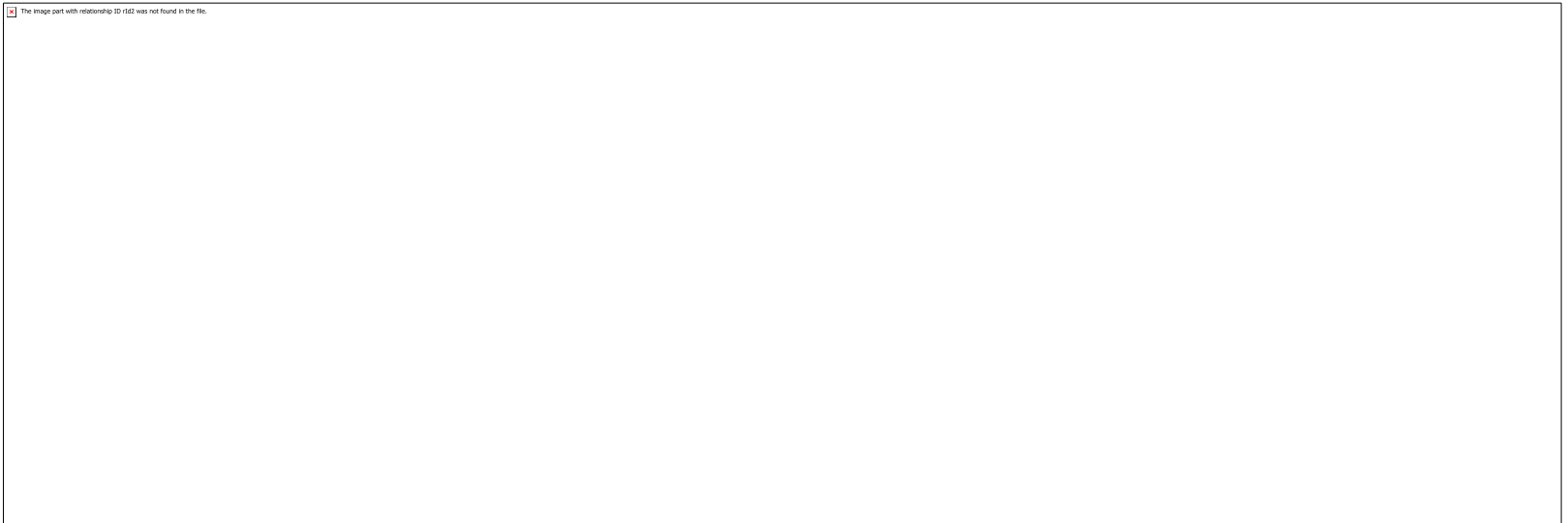
---

- Fundamentals of Deep Learning
  - Basic concepts and ideas in Deep Learning
  - Traditional machine learning vs Deep Learning
  - Advantages and problems of Deep Learning
- Deep Learning for Inverse Problems in Imaging
- Deep Learning based for Synthetic Aperture Imaging
- Conclusion

# Basic Concepts in Deep Learning

---

- Perceptron (Rosenblatt, 1957)

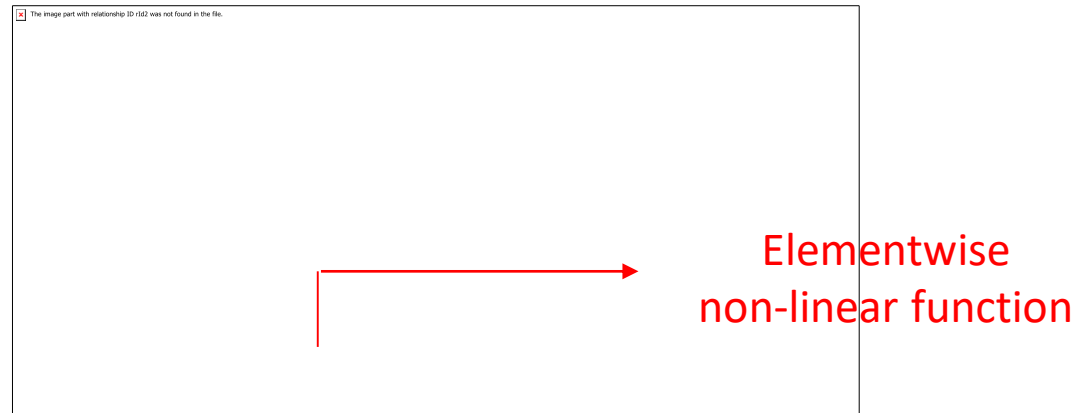



- Concept of a “neuron”
- Building block of machine learning methods

# Basic Concepts in DL - Layer

---

- Parallel implementation of neurons: “layer”
- **Layer** – A processing block



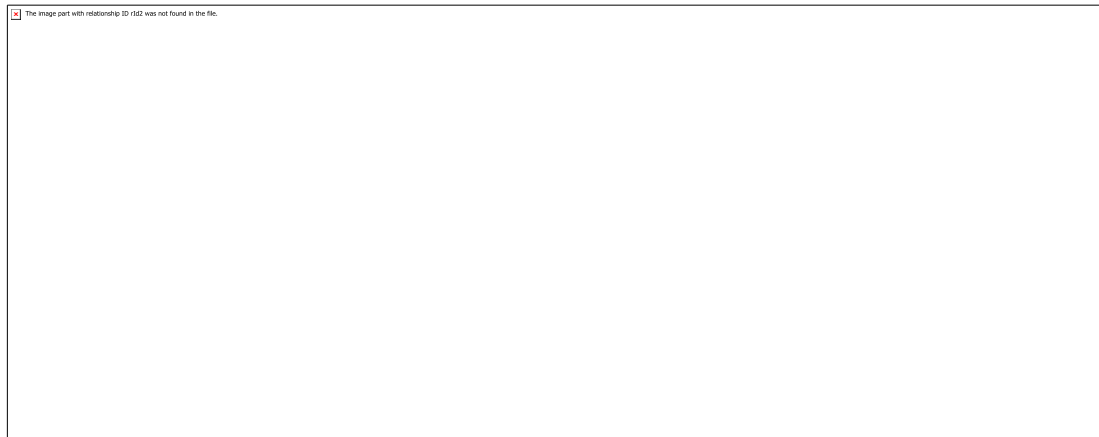
- Parametrized by a **matrix  $\mathbf{A}$**  and a **bias vector  $\mathbf{b}$**
-  called a representation of  $\mathbf{x}$  which lies in a “feature space”.



# Traditional Machine Learning

---

- Inductive learning – learn from examples
  - Classification: learning class boundaries in data
  - Regression: learn a function to fit data
- Classifiers are “shallow”, 2-layer architectures
- Features are hand crafted



# Deep Learning vs Traditional Machine Learning

---

- **More Layers** – Forward Propagation

- Many more layers – Deep Networks
- Each layer produces a representation of the output from the previous layer

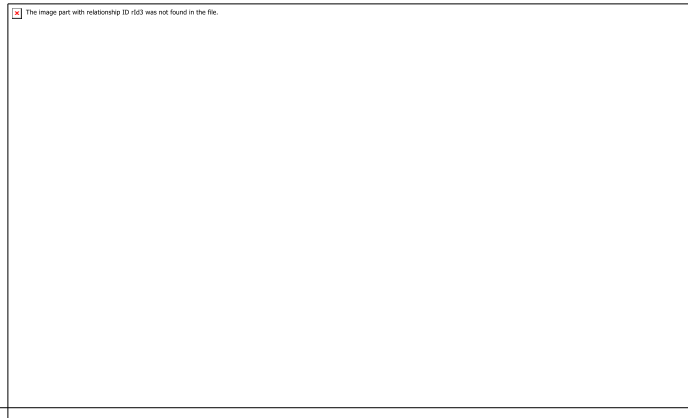


- **Hierarchical feature spaces** as features get more abstract
- Raw data processed directly – **no hand crafting of features beforehand**

# Breakthroughs in Deep Learning – Convolutional Networks

---

- First Convolutional Neural Network, 1980 (Fukushima)



LeCun, Bengio, and Hinton. "Deep learning" Nature 2015

# Breakthroughs in Deep Learning – Backpropagation

---

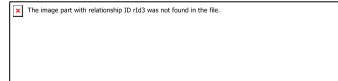
- Backpropagation algorithm, Hinton (1987)
- **Fundamental way of learning** in deep models



# Learning with Backpropagation

- “Train” with examples

- Network operator



- parametrized by the weight matrices and bias vectors



- “Learning”: estimating/updating network parameters so that produces desired output

- Given a set of data



and ground truth

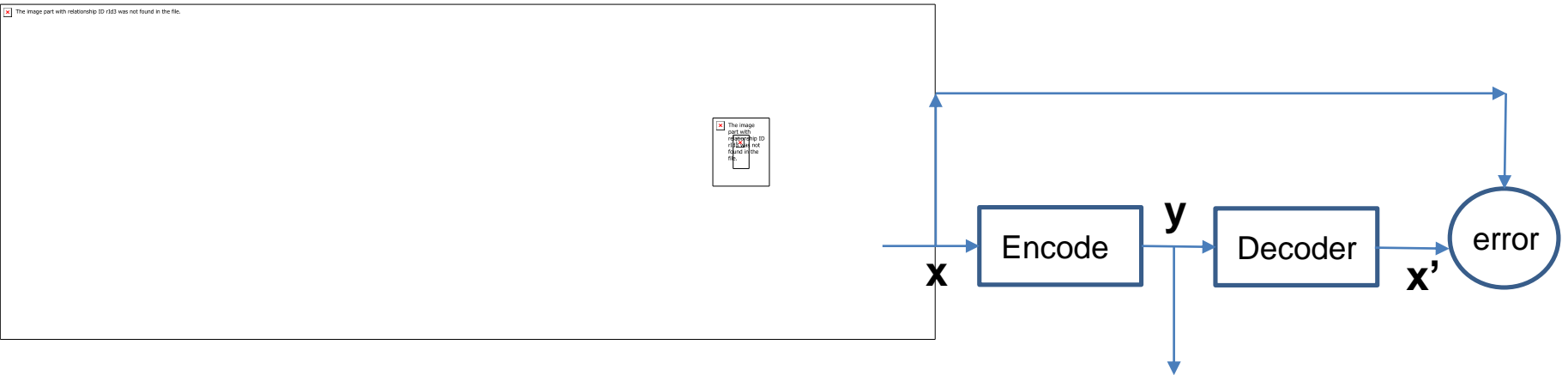
, update network parameters



Loss function ←



# Deep Learning Architectures



- **Recurrent Neural Networks (RNNs)**
  - Widely used in natural language processing and speech generation
  - Great imitators of iterative processes
- **Auto-encoders**
  - $\| \cdot \|^2$  of error is backpropagated for learning
  - Output layer folds back, suitable for denoising

# Breakthroughs in Deep Learning

---

- **LeNet-5, LeCun, Bottou, Bengio (1998)**
  - An improved CNN structure, demonstrated for character recognition.
- **Deep Belief Nets, Hinton (2006)**
  - Introduced the term "Deep Learning", and unsupervised pre-training
- **Deep Neural Network - Hidden Markov Models for speech recognition, Dong Yu, Microsoft (2011)**
  - Record breaking performance in speech recognition
- **AlexNet, Krizhevsky, Sutskever, Hinton (2012)**
  - Record breaking performance in ImageNet classification.

# Advantages of Deep Learning

---

- Big data
- Faster computation power
- Bypassing feature engineering
- Ability to approximate very complex mappings
- Learns goal driven representations
- Software infrastructure



# Problems in Deep Learning

---

- Learning is very high dimensional and highly **non-convex optimization**
- Many hyper-parameters and **heuristic tuning**
- Training **requires large data sets** and high **computation power**
- **Vague** theoretical understanding
- **Overfitting**, generality

# Outline

---

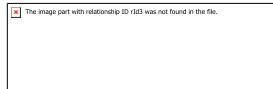
- Fundamentals of Deep Learning
- Deep Learning for Inverse Problems in Imaging
  - Image reconstruction as a machine learning task
  - Deep Learning as an inverse solver
  - Bayesian and optimization inspired Deep Learning
- Deep Learning based for Synthetic Aperture Imaging
- Conclusion

[1] Yonel, Bariscan, Eric Mason, and Birsen Yazıcı. "Deep learning for passive synthetic aperture radar." *IEEE Journal of Selected Topics in Signal Processing* 12.1 (2018): 90-103.

# Problems in Imaging

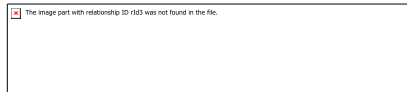
---

- **Forward model:** derived from underlying physics



- Can we **learn the model from** data via DL?

- **Inversion:** obtain estimate



- How can we **implement inversion methods with DL?**

- **Efficient algorithm design**

- Can DL offer **faster convergence?**

- **Automatic Target Recognition**

- Can we design DL based **inversion methods guided by the goals of ATR?**

# Deep Network as a Forward Solver

---

- **Conventional forward modeling** - Similar to 2-layer conventional machine learning



- **DL-based forward modeling** - Insert hidden layers



- Learn non-linear forward models from data
- Improve over linearized/idealized forward models
- Potential applications in high fidelity data generation

# Image Reconstruction as a Machine Learning Task

---

- **Image:** A desired representation of measurements in image space
- **Conventional image reconstruction:** Similar to 2-layer conventional machine learning
  - **Backprojection:** A representation of measurements in the range of adjoint operator



- **Deep Learning-based image reconstruction:** Use deep layers to form a new representation at each layer, progressively approaching to desired output

# Deep Network as an Inverse Solver

---

- Insert hidden layers



- "Model-free" inverse solver

- Learn the inverse mapping from training data



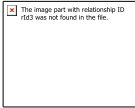
- Initialize network with physics-based backprojection, i.e.,



- Requires extensive training data to avoid over fitting

# Bayesian and Optimization Inspired DL-based Image Reconstruction

---

- How to choose the network non-linearity  ?
  - Based on **a priori information**
- Why?
  - Formulate reconstruction as **a constrained least square optimization problem**
  - Address optimization via **proximal gradient descent** method
- **Build layers of deep network from iterations** of a proximal gradient descent method
  - Affine mapping - Gradient descent step
  - Non-linearity - Proximity operator of the constraint

# Bayesian and Optimization Inspired DL-based Image Reconstruction

---

- **Bayesian formulation**

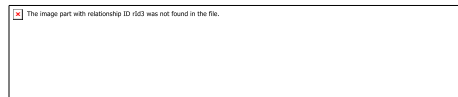


- **Proximal gradient descent**

- **Gradient descent** over the smooth  term:



- **Project onto the feasible set** of the regularization term





# RNN as a Proximal Gradient Descent Optimization

 The image part with relationship ID r163 was not found in the file.

- Rewriting

 The image part with relationship ID r163 was not found in the file.

 The image part with relationship ID r163 was not found in the file.

- Unfold a fixed number of iterations to obtain an RNN

– **Weight matrix:**

 The image part with relationship ID r163 was not found in the file.

→ filter

– **Bias vector:**

 The image part with relationship ID r163 was not found in the file.

→ backprojection

– **Activation function:**

 The image part with relationship ID r163 was not found in the file.

→ network non-linearity

# Deep Learning for Image Reconstruction

---

- Image reconstruction - viewed as learning a representation of measurements in image space
- DL framework suitable for blind deconvolution
- Refine the unknowns in the forward model and perform reconstruction simultaneously
  - Initialization – partially known forward model
  - Forward propagation – image reconstruction
  - Backpropagation – refinement of forward model
- Use training to drive the network towards goals and to learn the information implicit in the measurement data

# Outline

---

- Fundamentals of Deep Learning
- Deep Learning for Inverse Problems in Imaging
- Deep Learning based for Synthetic Aperture Imaging
  - Passive SAR Imaging
  - ATR-aware Synthetic Aperture Imaging
- Conclusion

# SAR Imaging

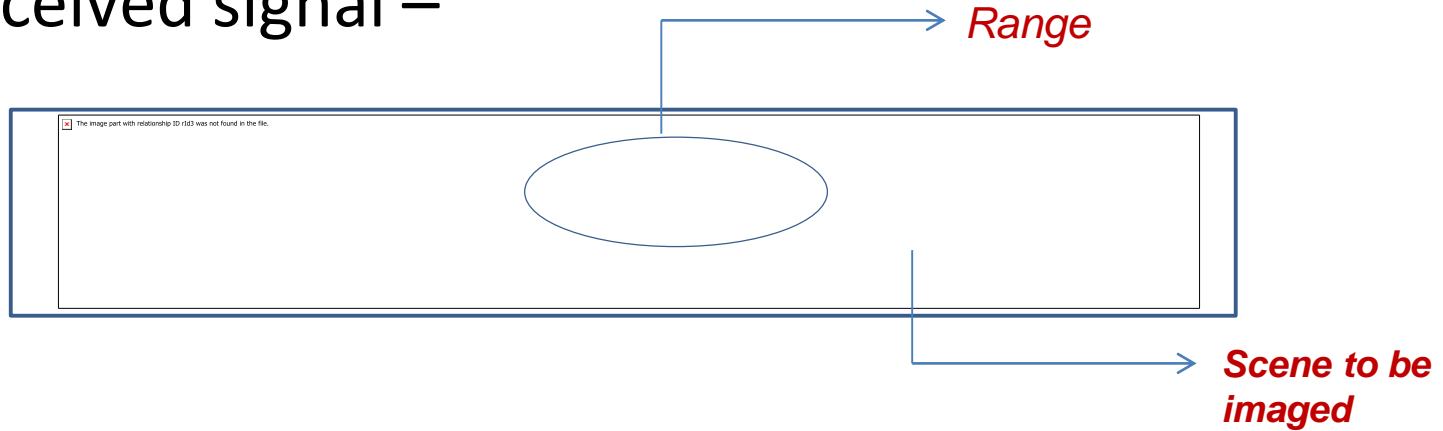
---

- Configurations (a) Monostatic, (b) Bistatic

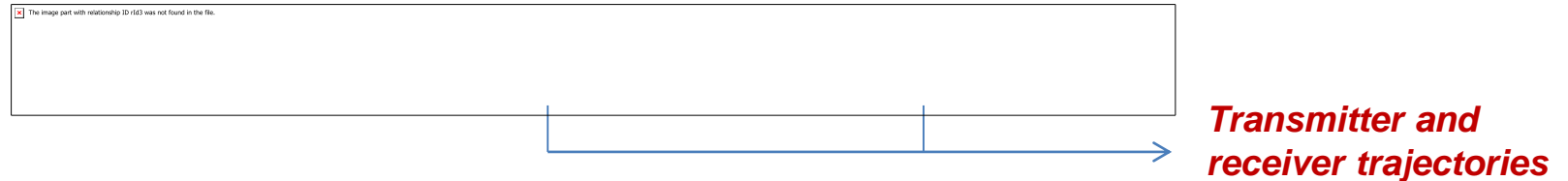


# SAR Forward Model

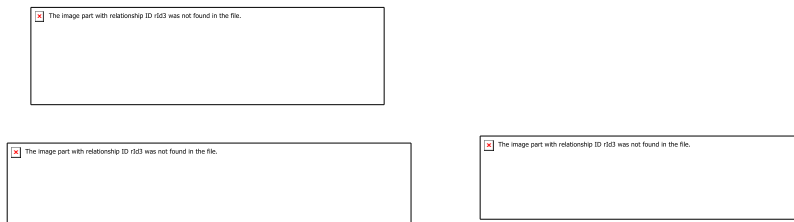
- Received signal –



*Bistatic range*



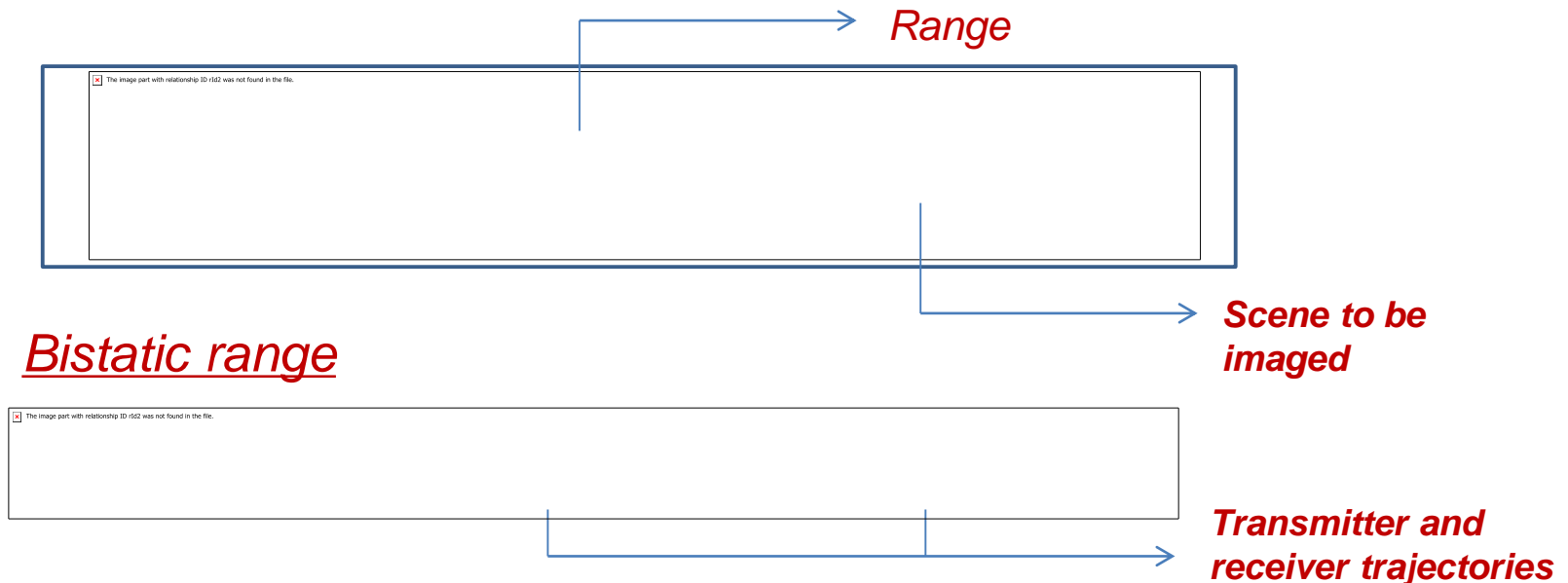
*Ground topography*



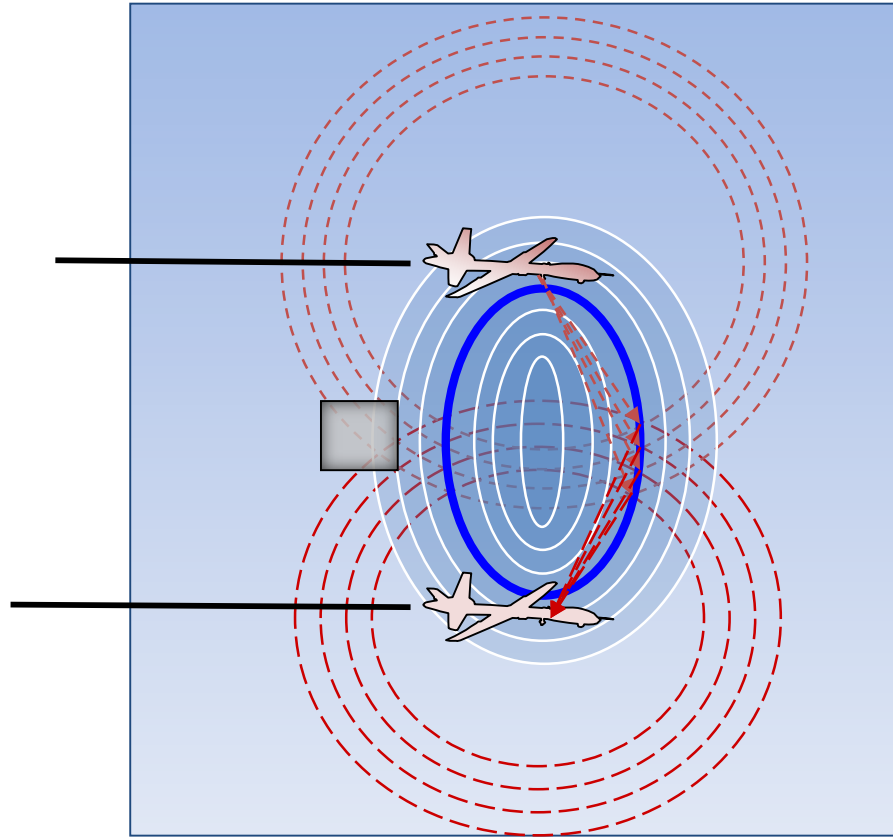
*Height*

# SAR Forward Model

- Measurements - **Generalized Radon Transform (GRT)** of scene reflectivity
  - GRT - **Filtered projections of reflectivity onto some smooth manifolds**
  - Manifold - Phase of the kernel
  - Weight - Amplitude of the kernel



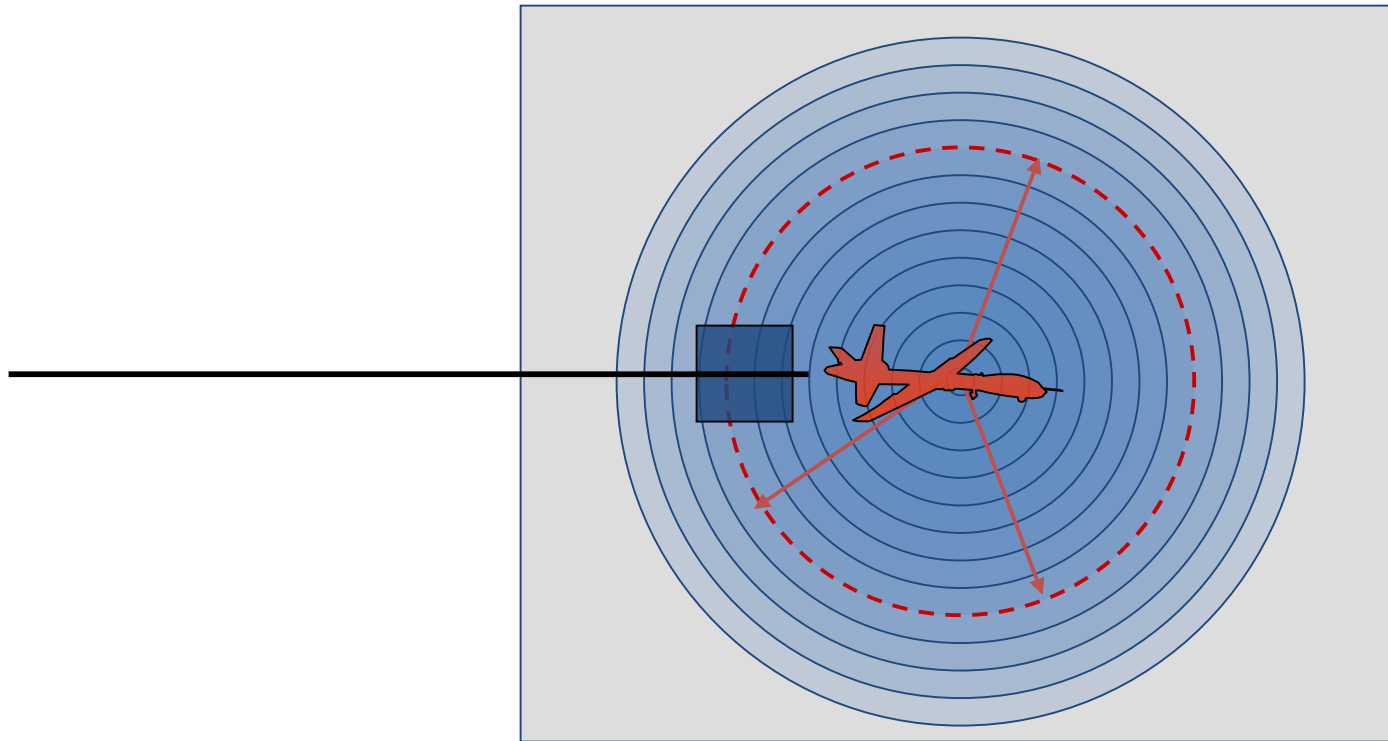
# Bi-static SAR Forward Model



- *Iso-range surfaces* - Ellipsoids
- *Iso-range contours* - Intersection of ellipsoids with topography
- Flat topography → Ellipses

# Mono-static SAR Forward Model

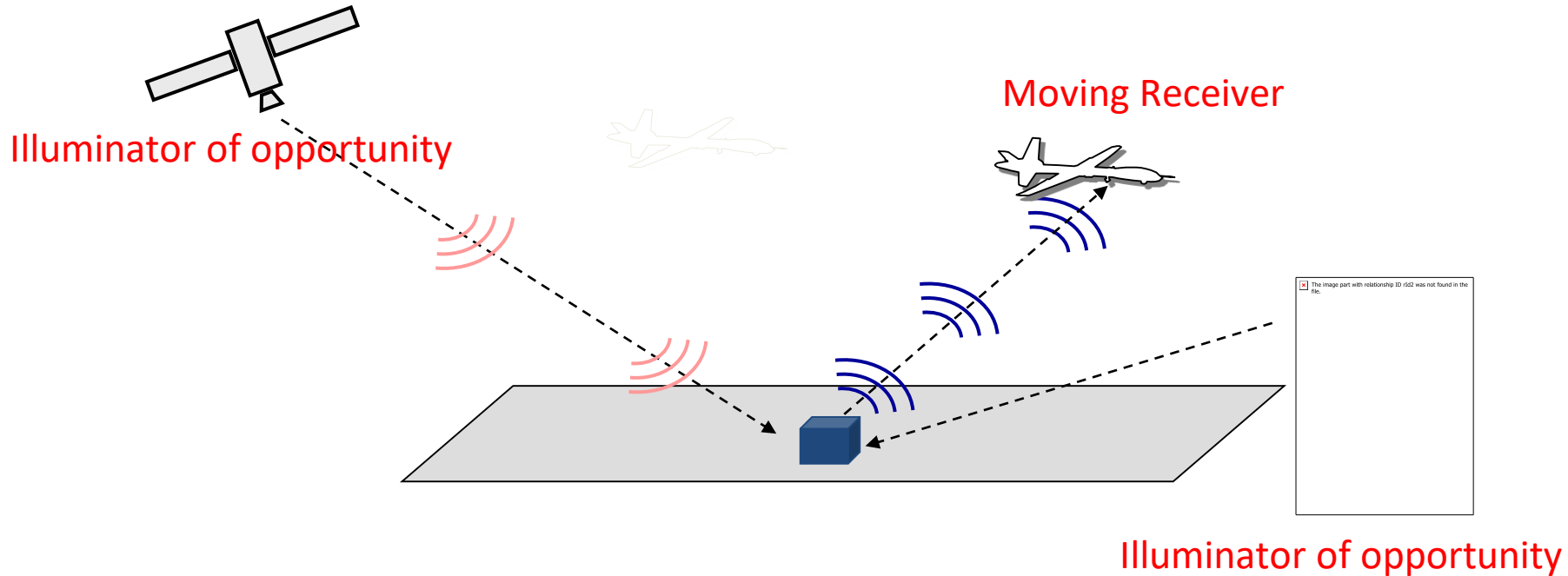
---



- *Iso-range surfaces* - Spheres
- *Iso-range contours* - Intersection of spheres with topography
- Flat topography → Circles



# Passive SAR



- Scene illuminated by transmitters of opportunity: TV, cell-phone stations etc.
- Receive only airborne antenna uses backscattered measurements to make an image of the scene

# Motivations and Challenges

---

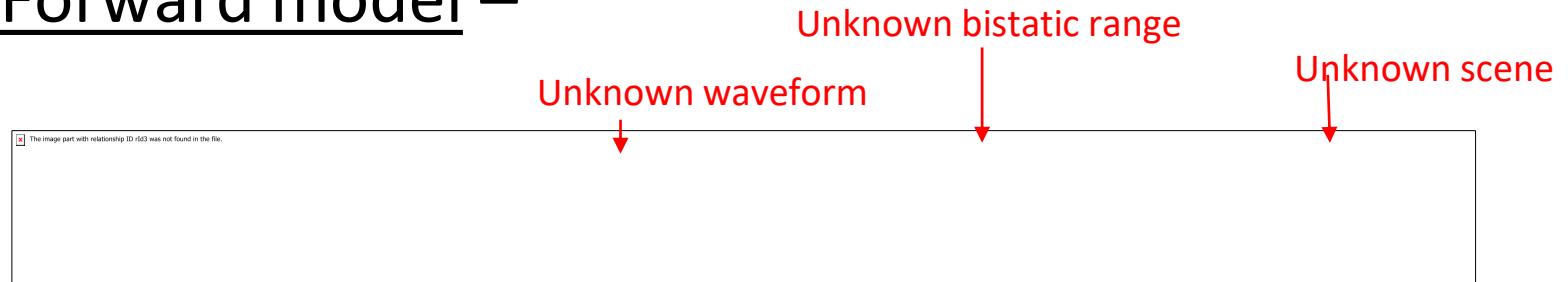
- Rapid growth in the number of RF sources of opportunity
  - *Radio signals, TV signals, communication signals, WiFi, WiMAX...*
- Requires receivers only
  - *Inexpensive, mobile, versatile, and suitable for rapid deployment*
  - Less vulnerable to electronic counter measures

## Challenges

- Transmitter is not in user control
- The location of the transmitter may not be known
- Waveforms may not have sufficient bandwidth

# Passive Synthetic Aperture Imaging [1,2]

- Forward model –



- Model –



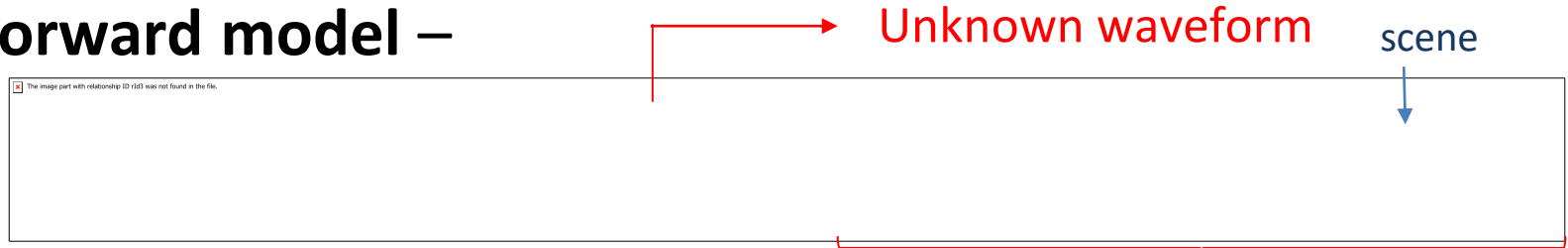
- Discretized model –  $\mathbf{d} \approx \mathbf{F}\mathbf{p} + \text{noise}$
- Neither  $\mathbf{F}$  nor  $\mathbf{p}$  is known – **Blind deconvolution**

[1] Yonel, Bariscan, Eric Mason, and Birsen Yazıcı. "Deep learning for passive synthetic aperture radar." *IEEE Journal of Selected Topics in Signal Processing* 12.1 (2018): 90-103.

[2] Yonel, Bariscan, Eric Mason, and Birsen Yazıcı. "Deep Learning for Waveform Estimation and Imaging in Passive Radar." *in the special issue of IET on High Resolution Passive Imaging*, 2019.

# Passive Synthetic Aperture Radar

- **Forward model –**

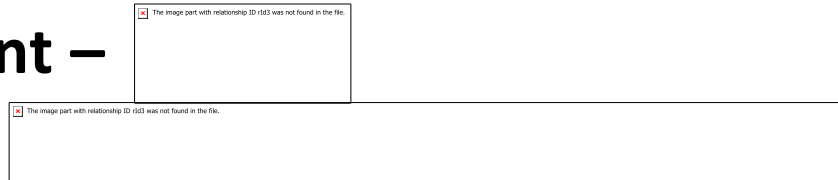


- **Discretize the scene –**



- **Known component –**

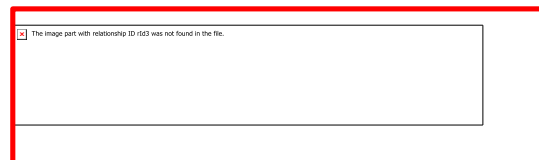
- Bistatic range –



- Geometric spreading –



- **Discretized forward model –**



# Network Parametrization and Backpropagation

---

- **Network architecture** – Recurrent auto-encoder

- **Network parameters** –

- Bias –

- Filter –

- **Network operator** approximates an identity operator

- Train the network in an unsupervised manner to estimate

# Training by Projected Stochastic Gradient Descent

---

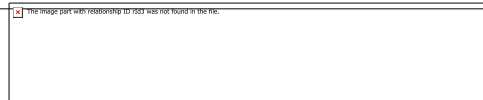
- Network operator –



- Learn  $\mathbf{w}$  and  $\lambda$  by minimizing



given training set



- Include prior information on  $\mathbf{w}$  and  $\lambda$ ; in the form of constraints.
- Minimize by projected SGD of the form:

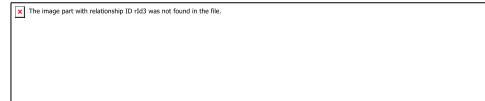
# Training by Projected Stochastic Gradient Descent

---

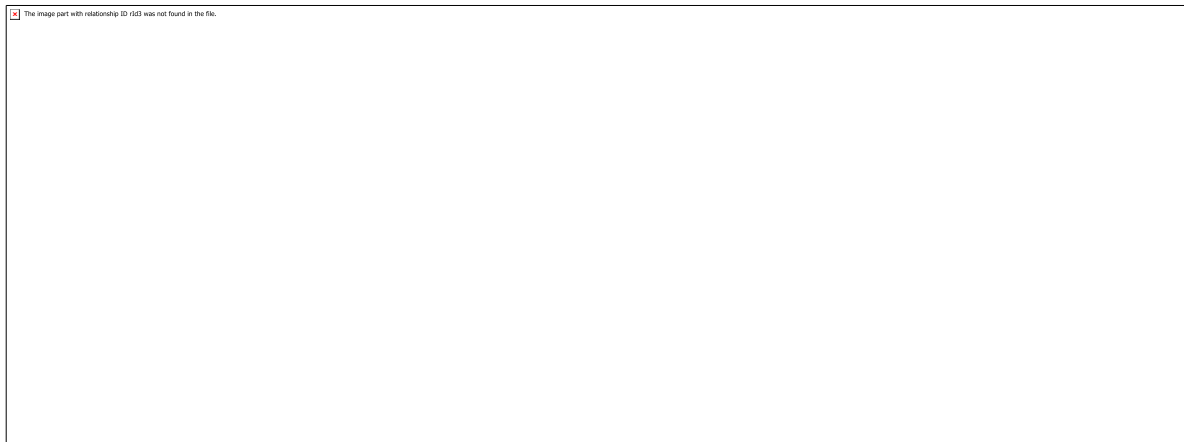
- Learn  $\mathbf{w}$  and  $\lambda$  by minimizing



given training set



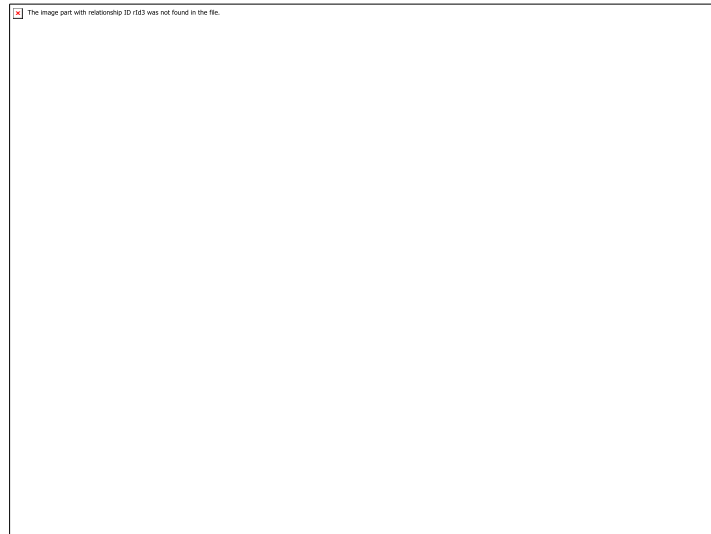
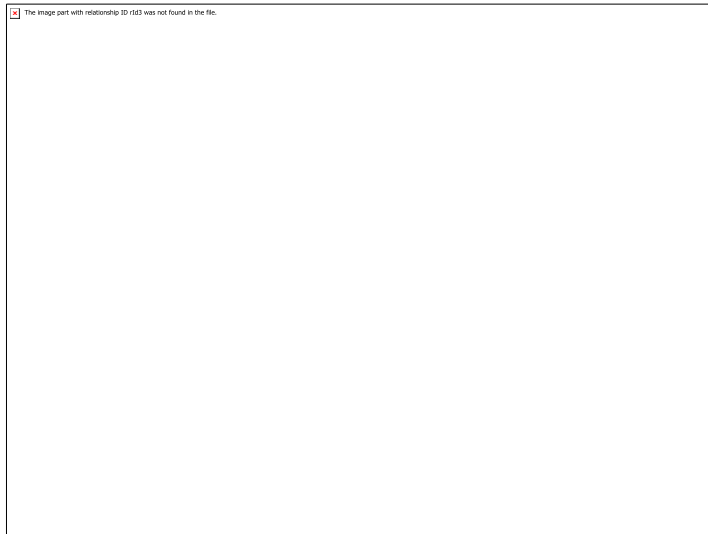
- Include prior information on  $\mathbf{w}$  and  $\lambda$ ; in the form of constraints and update by stochastic gradient descent



# Numerical Simulations

---

- Bandwidth = 8 MHz,  $f_c = 760$  MHz
- Unknown transmitted waveform = QPSK signal,  $A=1$
- 620 x 620 meter flat scene,
- 20m range resolution, 32 x 32 pixels
- Initialization of  $\mathbf{w}$ : random QPSK symbols




**Figure:** *Ground truth and image reconstructed with initial guess for the QPSK waveform*



# Numerical Simulations

---

## Network Properties

- 
- Number of layers  $L = 4$
- Training size  $T = 10$
- Number of epochs  $I = 1, 2, \dots, 10$
- Initial learning rate  $\eta_0 = 1e - 4, \eta_{I+1} = \eta_I / (I + 1)$
- Threshold ( $\tau = \alpha\lambda$ ) learning rate  $\eta_I \times 1e - 7$

# Numerical Simulations

---

- Different SNR levels for training and test data: -15, -10, -5, 0 dB SAR measurements.
- Training set: Sparse scene with single extended target of varying rectangular shape and location.
- Length and width: picked randomly in  $[1,6] \times [1,6]$  range.
- Target placement: random in  $[3,28] \times [3,28]$  range of pixels.
- Test set: 20 different realization of SAR measurements of the scene of interest under corresponding training noise level.

# Numerical Simulations

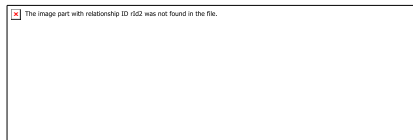
---

## Figures of merit

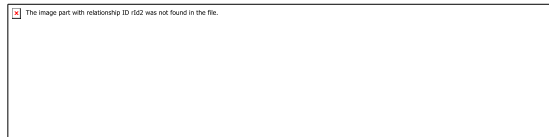
- Data Mismatch



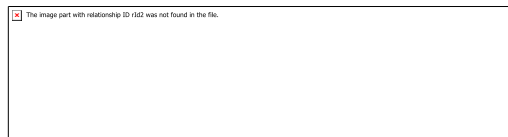
- Image domain error



- Image contrast



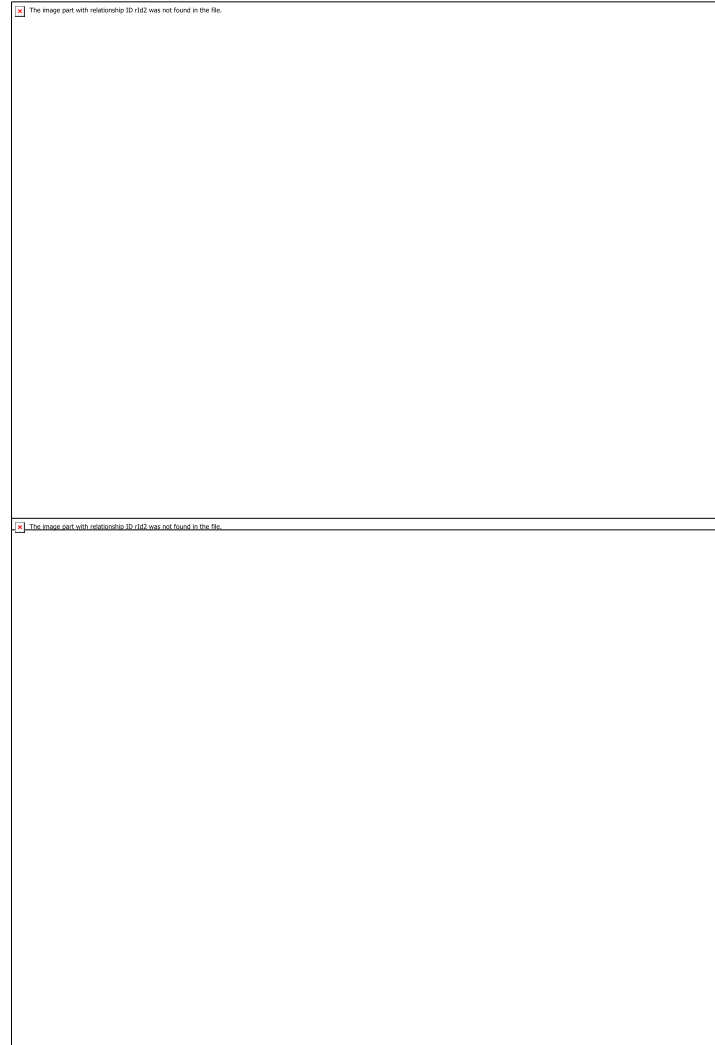
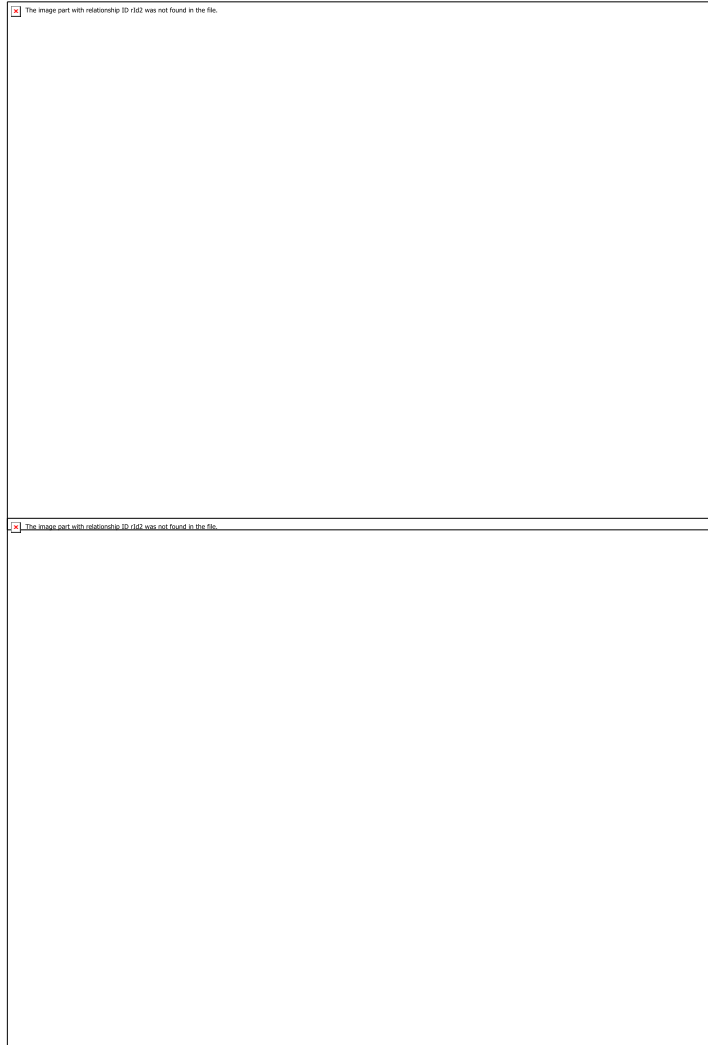
- Waveform error



# Numerical Simulations

---

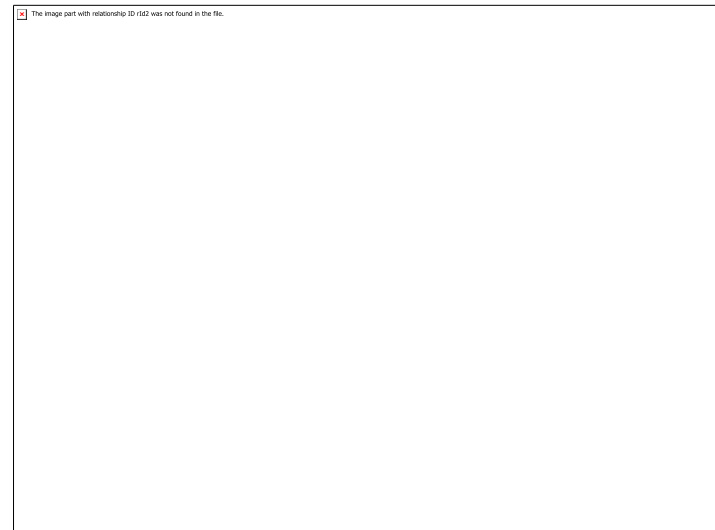
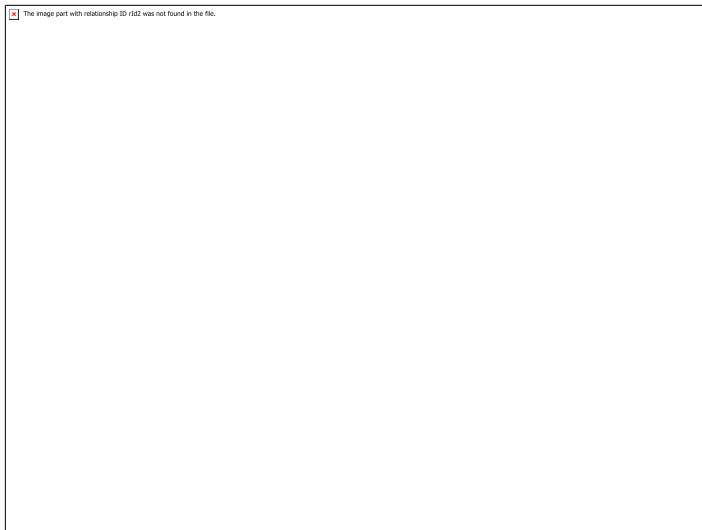
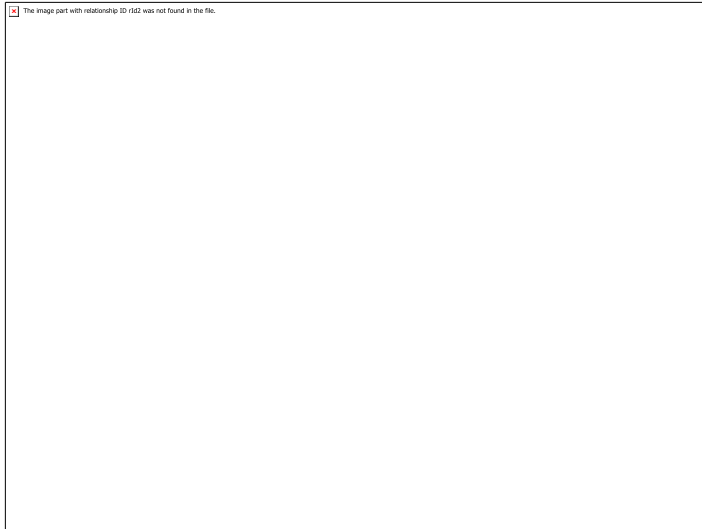
## Reconstructed Images from the Test Set



# Numerical Simulations

---

## Error Curves: Data Mismatch, Image Mismatch, Contrast, Waveform Error



# Outline

---

- Fundamentals of Deep Learning
- Deep Learning for Inverse Problems in Imaging
- Deep Learning based for Synthetic Aperture Imaging
  - Passive SAR Imaging
  - ATR-aware Synthetic Aperture Imaging
- Conclusion

# ATR Directly from Received Signal bypassing Image Reconstruction [3]

---

- DL has shown staggering performance in ATR applications from images
- Conventional approach



- ATR directly from received signal





- Combine ATR and image reconstruction into a single step to
  - Reduce computational complexity
  - Improve ATR performance

# Network Architecture Inspired by Sparse Dictionary Learning

The image part with relationship ID r04 was not found in the file.

- Inspired by **classification via sparse representation**
- **Underlying optimization problem:**

The image part with relationship ID r04 was not found in the file.

-  – Dictionary: **A set of basis vectors along the columns of a matrix**
-  – sparse coefficient: **Represents samples of its own category more sparsely than samples from a different category**

The image part with relationship ID r04 was not found in the file.

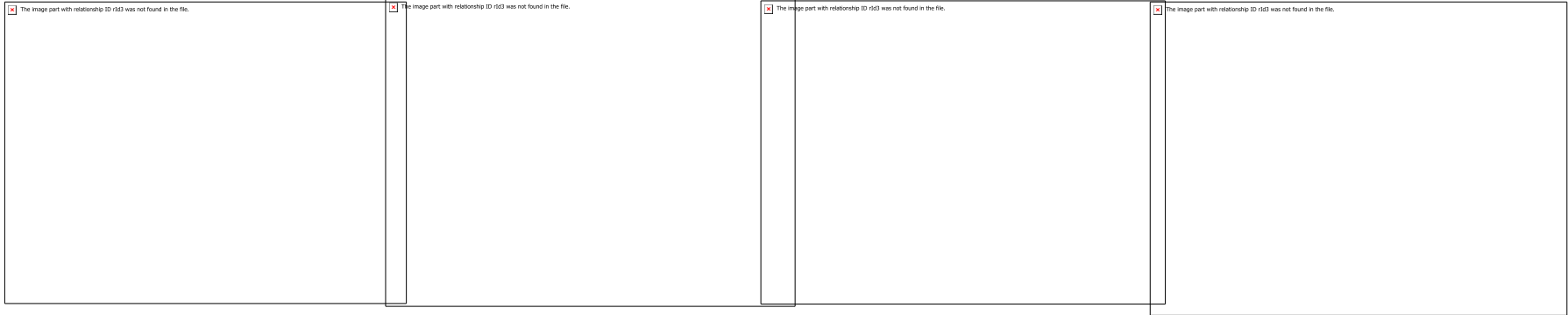
and

The image part with relationship ID r04 was not found in the file.

-  – Network weights → **Function of D**
-  – Non-linear function



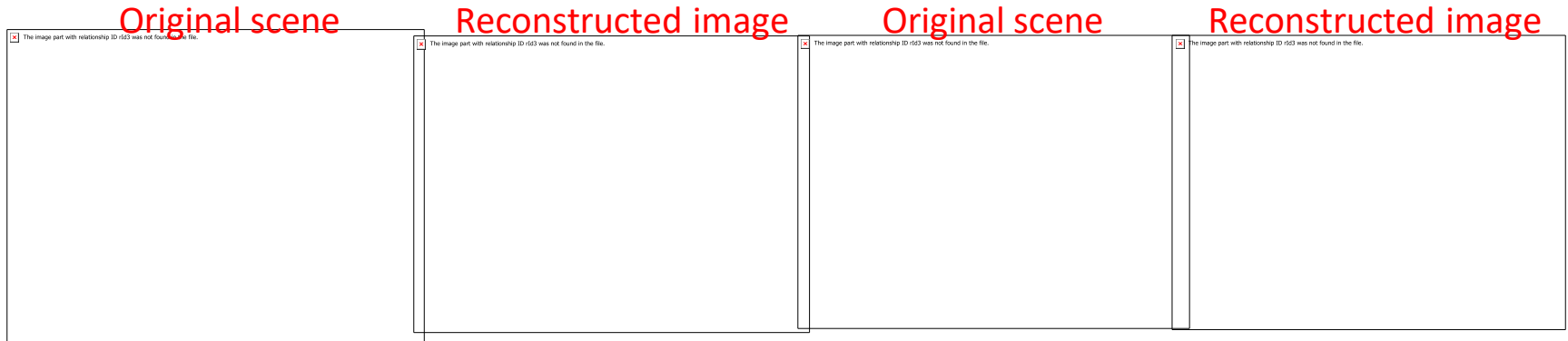
# Numerical Simulations



Sample scenes with square and triangular objects

- **Significantly sparsely sampled imaging data** - No. of **slow-time** and **fast-time** samples – **4** and **20** , respectively
  - Random scenes are synthesized by placing two types of objects at different locations, orientations and on different backgrounds.
- 
- Training set: 28x28 pixels with single extended target of rectangular and triangular shape.
  - Target placement: random in  $[1,25] \times [1,25]$  range of pixels.
  - No. of dictionary columns – **200**

# Numerical Simulations

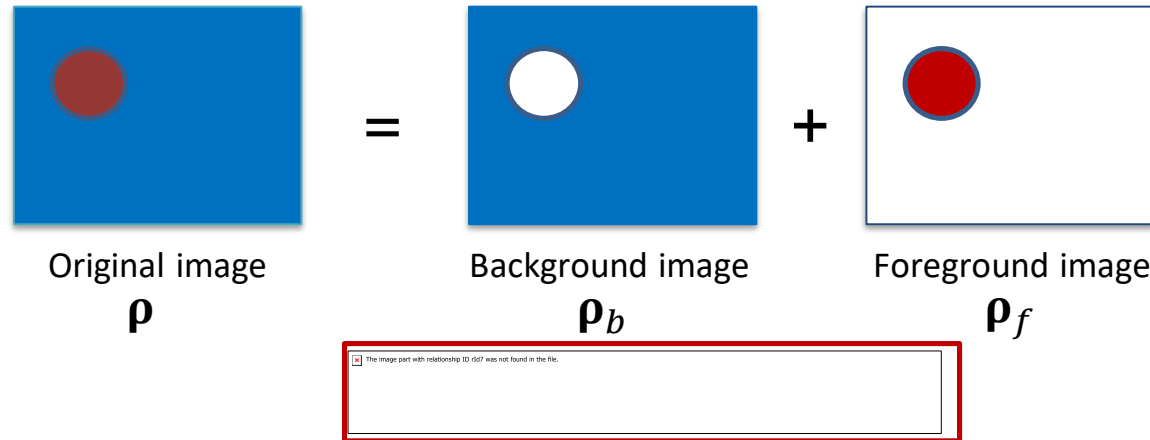


- **Polar format reconstruction followed by sparse dictionary method -**

SNR (dB)	Classification accuracy (%)	
	DL classification	Image reconstruction + classification
-3	84.6	50.7
0	90.2	50.8
3	91.6	52

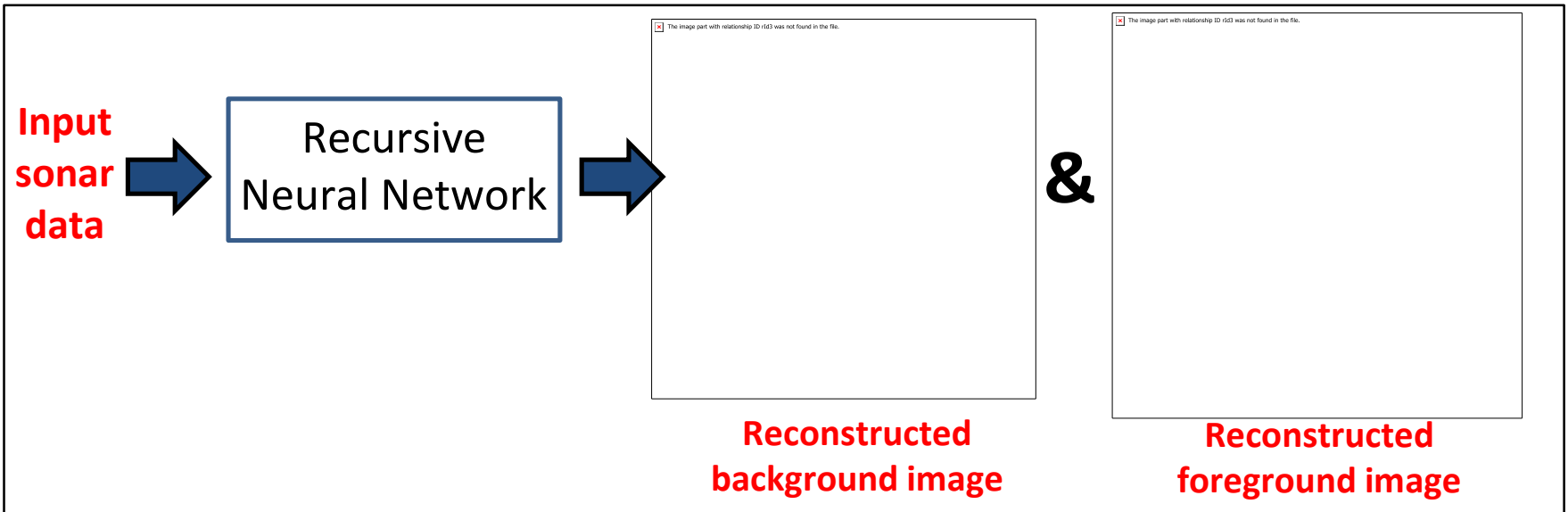
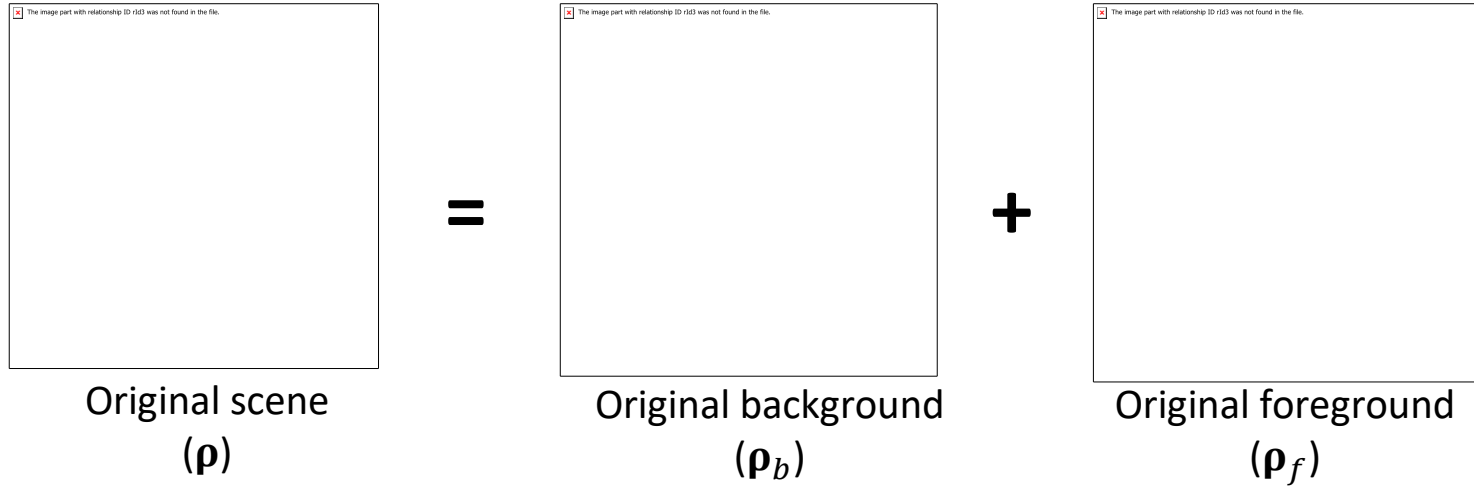
# Reconstruction of Foreground/Background Images

---

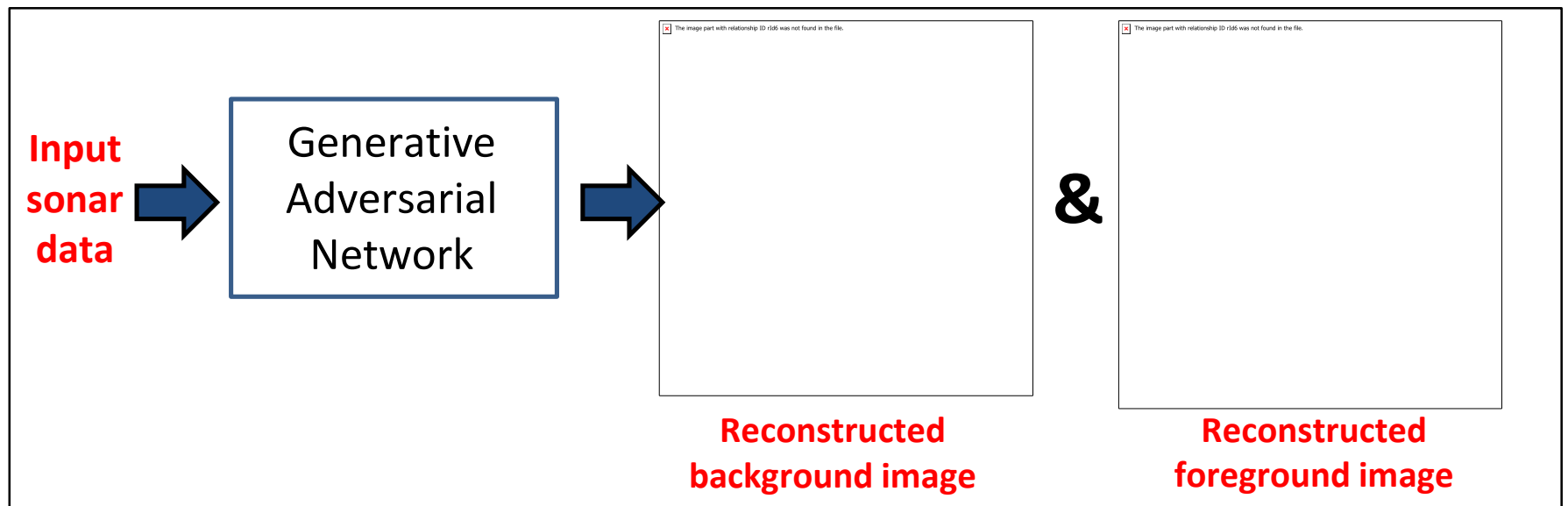
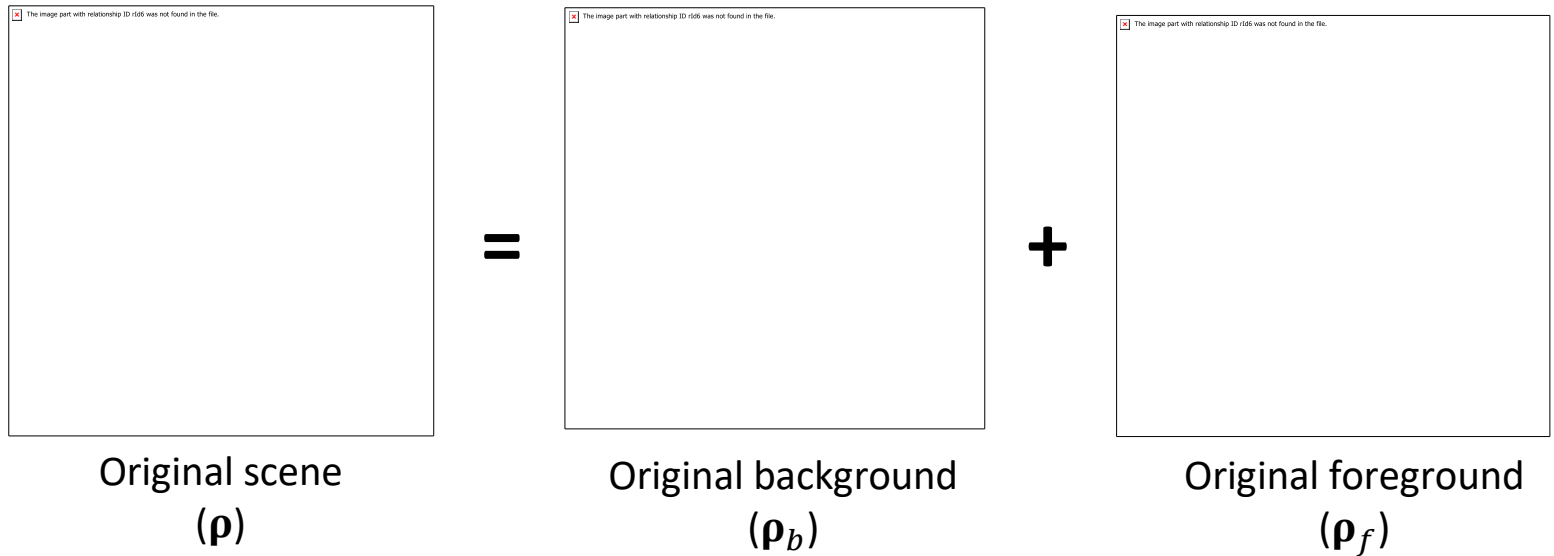


- Reconstruct two images:
  - A foreground image  $\rho_f$  including one or more objects of interest (mines) and
  - A background image,  $\rho_b$
- Two approaches:
  - Supervised: Training –  $\mathbf{d}$ ,  $\rho_f$  and  $\rho_b$  available, Testing – Only  $\mathbf{d}$  is available
  - Unsupervised: Training –  $\mathbf{d}$  and **label** available, Testing – Only  $\mathbf{d}$  is available

# Numerical Simulations - Supervised

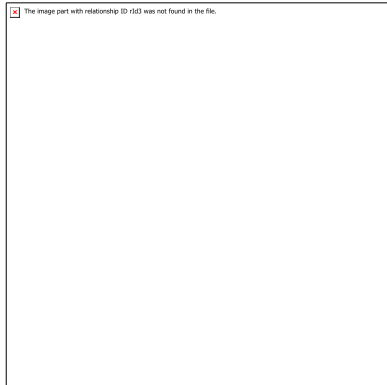


# Numerical Simulations - Unsupervised

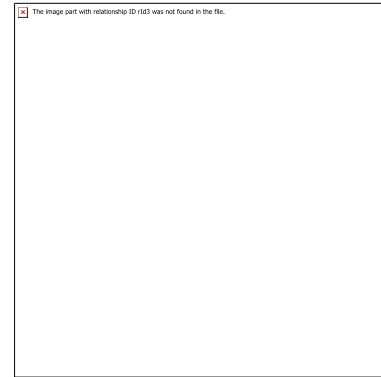
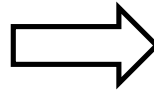


# Comparison with Conventional Approach

- **Foreground separation using proposed model**

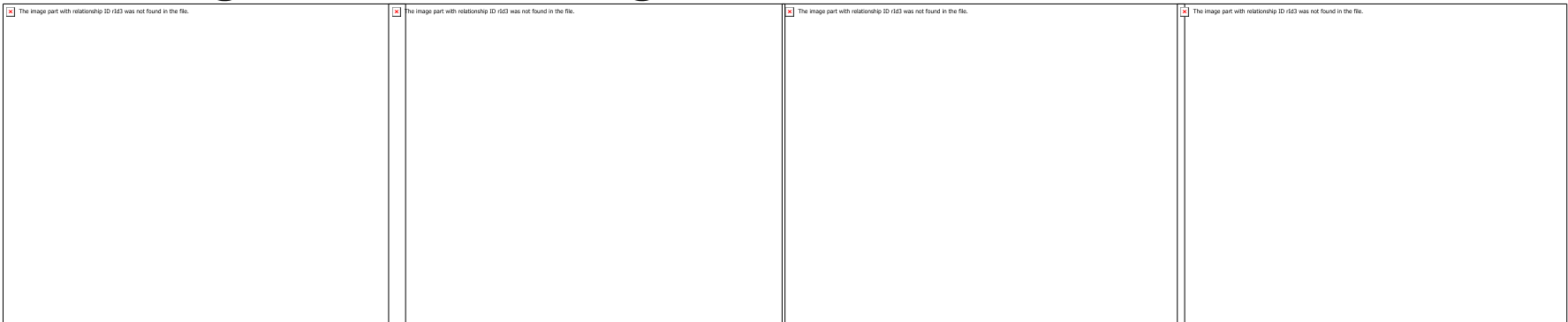


**Original image**



**Reconstructed foreground image**

- **Image formation + edge detector**



**'Canny' edge  
detection**

**'Sobel' edge  
detection**

**'Roberts' edge  
detection**

**'LoG' edge detection**

# Conclusions

---

- DL framework: **a joint estimation & classification** tool for blind deconvolution combining a model based and data driven approaches
- **Accurate reconstruction performance**: good geometric fidelity, background suppression. Accurate estimation of the waveform only given a priori functional form
- **Classification** using sparse synthetic aperture data **directly from received sparse signal**
- Accurate **reconstruction of background and foreground images** from sparse received data